

# CS 4300: Compiler Theory

## Chapter 4 Syntax Analysis

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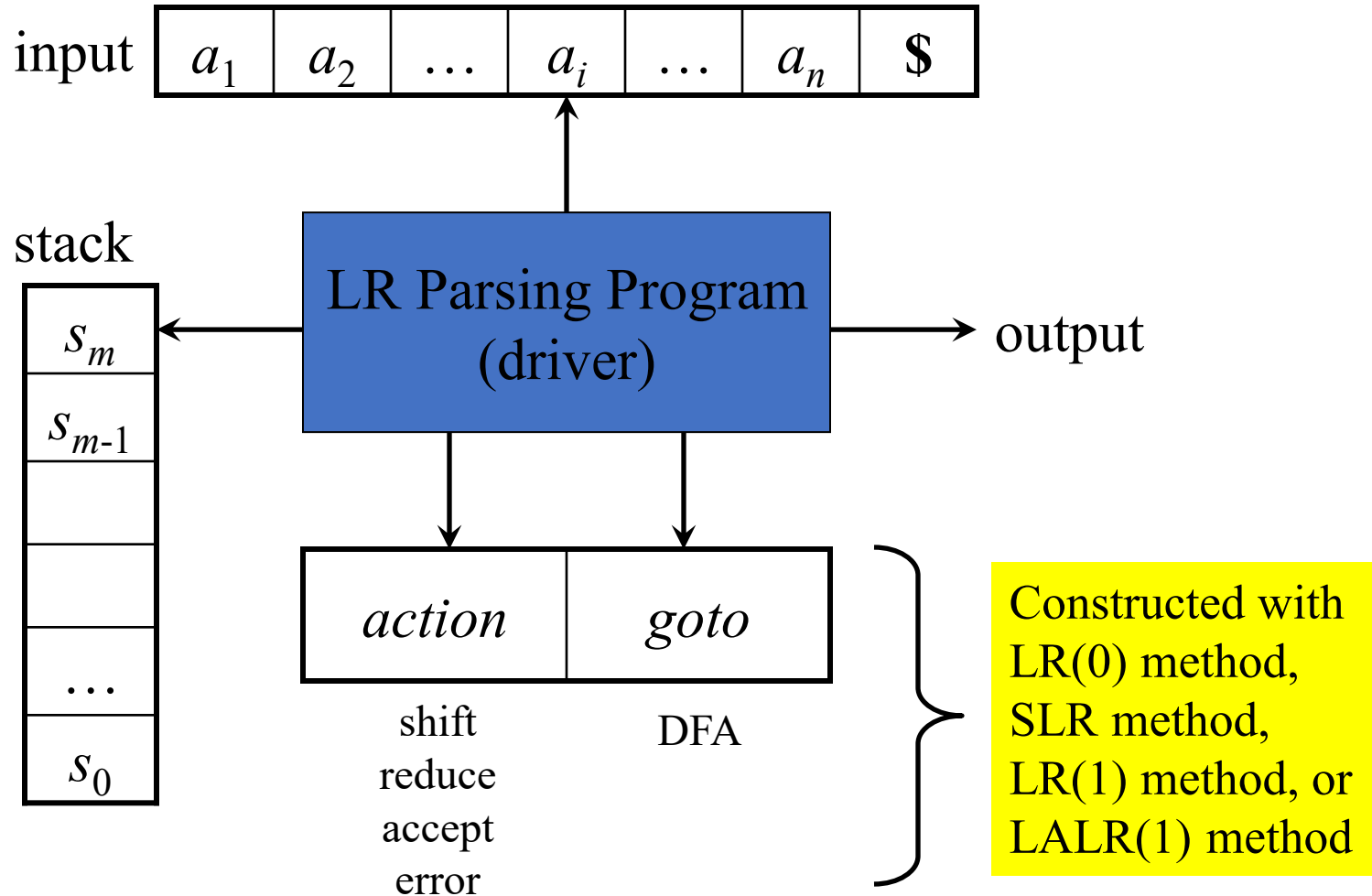
# Outlines (Sections)

1. Introduction
2. Context-Free Grammars
3. Writing a Grammar
4. Top-Down Parsing
5. Bottom-Up Parsing
6. Introduction to LR Parsing: Simple LR
7. More Powerful LR Parsers
8. Using Ambiguous Grammars
9. Parser Generators

# Quick Review of Last Lecture

- Bottom-Up Parsing
  - Stack Implementation of Shift-Reduce Parsing
  - Shift-reduce and reduce-reduce conflicts
- LR Parsing
  - LR(0) Items of a Grammar
  - The closure Operation for LR(0) Items
  - The goto Operation for LR(0) Items
  - Construct LR(0) Automaton of a Grammar
  - Use of the LR(0) Automaton
  - Examples

# Model of an LR Parser



# LR Parsing (Driver)

$X_1 X_2 \dots X_m a_i a_{i+1} \dots a_n$  ← right-sentential form

Configuration (= LR parser state):

$(\underbrace{s_0 s_1 s_2 \dots s_m}_{stack}, \underbrace{a_i a_{i+1} \dots a_n \$}_{input})$

**If**  $action[s_m, a_i] = \text{shift } s$  **then** push  $s$ , and advance input:

$(s_0 s_1 s_2 \dots s_m s, a_{i+1} \dots a_n \$)$

**If**  $action[s_m, a_i] = \text{reduce } A \rightarrow \beta$  and  $goto[s_{m-r}, A] = s$  with  $r=|\beta|$  **then** pop  $r$  symbols, and push  $s$ :

$(s_0 s_1 s_2 \dots s_{m-r} s, a_i a_{i+1} \dots a_n \$)$

**If**  $action[s_m, a_i] = \text{accept}$  **then** stop

**If**  $action[s_m, a_i] = \text{error}$  **then** attempt recovery

# Example LR(0) Parsing Table

State  $I_0$ :  
 $C' \rightarrow \bullet C$   
 $C \rightarrow \bullet A B$   
 $A \rightarrow \bullet a$

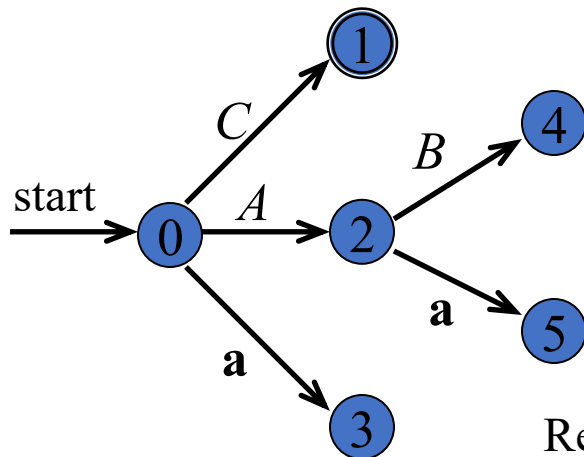
State  $I_1$ :  
 $C' \rightarrow C \bullet$

State  $I_2$ :  
 $C \rightarrow A \bullet B$   
 $B \rightarrow \bullet a$

State  $I_3$ :  
 $A \rightarrow a \bullet$

State  $I_4$ :  
 $C \rightarrow A B \bullet$

State  $I_5$ :  
 $B \rightarrow a \bullet$



Shift & goto 3

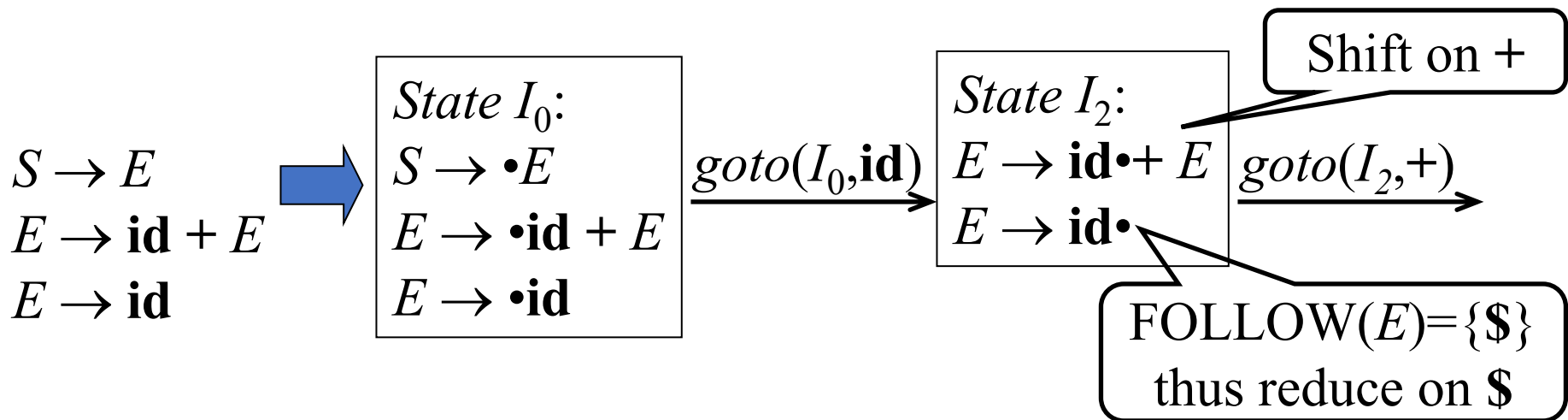
Reduce by  
production #2

state	action		goto		
	a	\$	C	A	B
0	s3		1	2	
1		acc			
2	s5				4
3	r3	r3			
4	r2	r2			
5	r4	r4			

Grammar:  
 1.  $C' \rightarrow C$   
 2.  $C \rightarrow A B$   
 3.  $A \rightarrow a$   
 4.  $B \rightarrow a$

# SLR Grammars

- SLR (Simple LR): SLR is a simple extension of LR(0) shift-reduce parsing
- SLR eliminates some conflicts by populating the parsing table with reductions  $A \rightarrow \alpha$  on symbols in  $\text{FOLLOW}(A)$



# SLR Parsing Table

- Reductions do not fill entire rows
- Otherwise the same as LR(0)

1.  $S \rightarrow E$
2.  $E \rightarrow \mathbf{id} + E$
3.  $E \rightarrow \mathbf{id}$

Shift on +

FOLLOW( $E$ ) = { $\$$ }  
thus reduce on  $\$$

	id	+	\$	$E$
0	s2			1
1			acc	
2		s3	r3	
3	s2			4
4			r2	

*State  $I_0$ :*

$S \rightarrow \bullet E$

$E \rightarrow \bullet \mathbf{id} + E$

$E \rightarrow \bullet \mathbf{id}$

*State  $I_2$ :*

$E \rightarrow \mathbf{id} \bullet + E$

$E \rightarrow \mathbf{id} \bullet$

*State  $I_1$ :*

$S \rightarrow E \bullet$

*State  $I_3$ :*

$E \rightarrow \mathbf{id} + \bullet E$

*State  $I_4$ :*

$E \rightarrow \mathbf{id} + E \bullet$



# SLR Parsing

- An LR(0) state is a set of LR(0) items
- An LR(0) item is a production with a • (dot) in the right-hand side
- Build the LR(0) DFA by
  - *Closure operation* to construct LR(0) items
  - *Goto operation* to determine transitions
- Construct the SLR parsing table from the DFA
- LR parser program uses the SLR parsing table to determine shift/reduce operations

# Constructing SLR Parsing Tables

1. Augment the grammar with  $S' \rightarrow S$
2. Construct  $C = \{I_0, I_1, \dots, I_n\}$ , the collection of sets of *LR(0) items*. State  $i$  is constructed from  $I_i$ .
3. If  $[A \rightarrow \alpha \bullet a \beta] \in I_i$  and  $\mathbf{goto}(I_i, a) = I_j$  then set  $\mathbf{action}[i, a] = \text{shift } j$ , where  $a$  is a terminal
4. If  $[A \rightarrow \alpha \bullet] \in I_i$  then set  $\mathbf{action}[i, a] = \text{reduce } A \rightarrow \alpha$  for all  $a \in \text{FOLLOW}(A)$  (apply only if  $A \neq S'$ )
5. If  $[S' \rightarrow S \bullet]$  is in  $I_i$  then set  $\mathbf{action}[i, \$] = \text{accept}$
6. If  $\mathbf{goto}(I_i, A) = I_j$  then set  $\mathbf{goto}[i, A] = j$
7. Repeat 3-6 until no more entries added
8. The initial state  $i$  is the  $I_i$  holding item  $[S' \rightarrow \bullet S]$

# Example Grammar and LR(0) Items

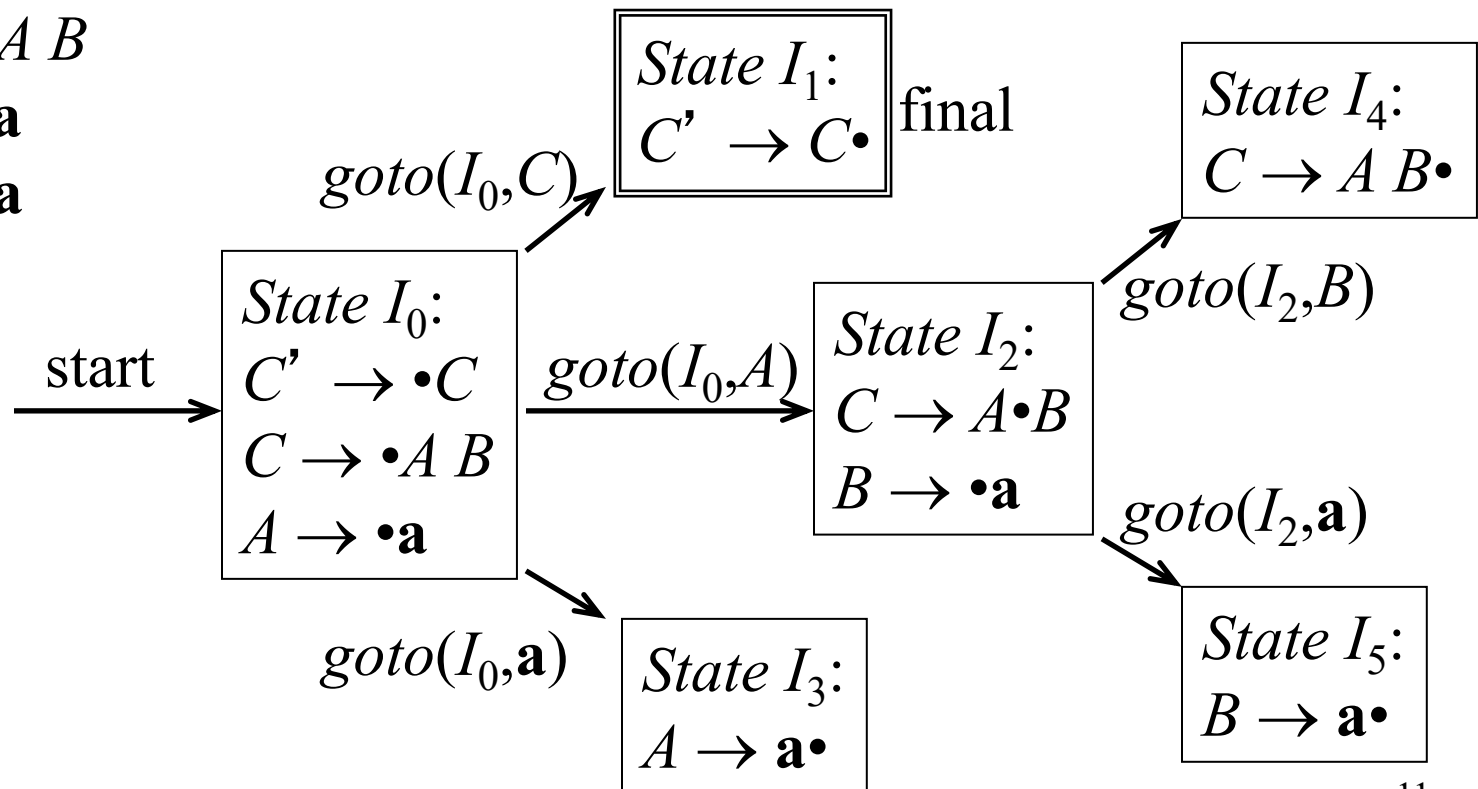
Augmented  
grammar:

1.  $C' \rightarrow C$
2.  $C \rightarrow A B$
3.  $A \rightarrow a$
4.  $B \rightarrow a$

$$I_0 = \text{closure}(\{[C' \rightarrow \bullet C]\})$$

$$I_1 = \text{goto}(I_0, C) = \text{closure}(\{[C' \rightarrow C \bullet]\})$$

...



# Example SLR Parsing Table

State  $I_0$ :  
 $C' \rightarrow \bullet C$   
 $C \rightarrow \bullet A B$   
 $A \rightarrow \bullet a$

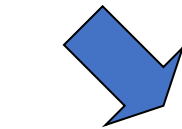
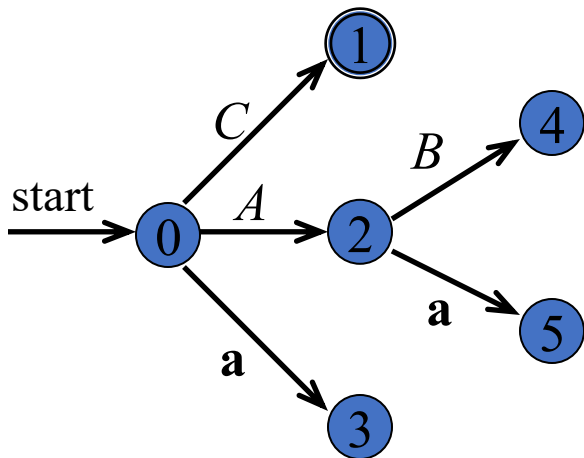
State  $I_1$ :  
 $C' \rightarrow C \bullet$

State  $I_2$ :  
 $C \rightarrow A \bullet B$   
 $B \rightarrow \bullet a$

State  $I_3$ :  
 $A \rightarrow a \bullet$

State  $I_4$ :  
 $C \rightarrow A B \bullet$

State  $I_5$ :  
 $B \rightarrow a \bullet$



state	action		goto		
	a	\$	C	A	B
0	s3		1	2	
1		acc			
2	s5				4
3	r3				
4		r2			
5		r4			

Grammar:

- $C' \rightarrow C$
- $C \rightarrow A B$
- $A \rightarrow a$
- $B \rightarrow a$

FOLLOW(A) = {a}

FOLLOW(C) = {\$}

FOLLOW(B) = {\$}

LR(0)  
Automaton  
for expression

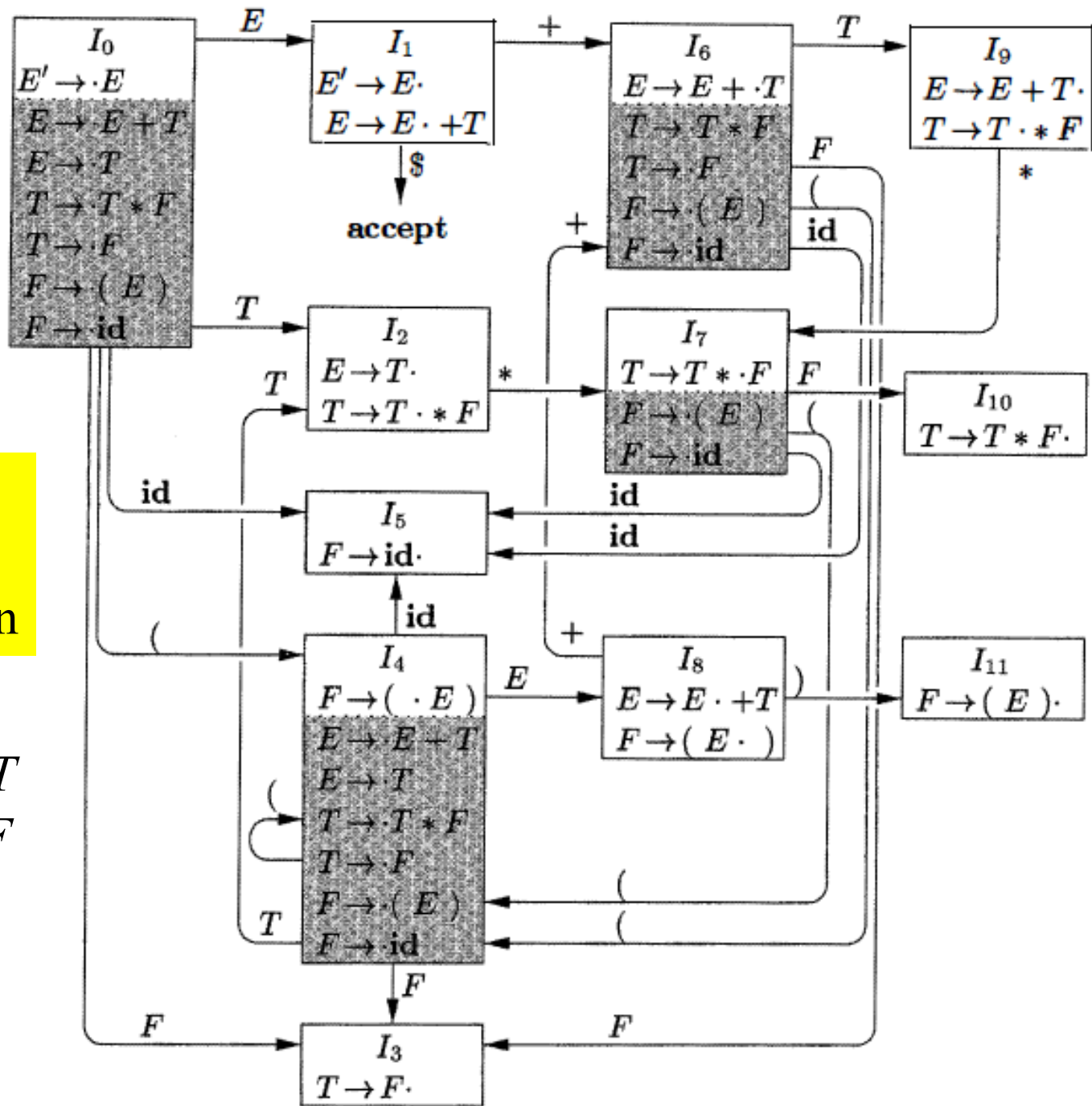
Grammar:

$E \rightarrow E + T \mid T$

$T \rightarrow T * F \mid F$

$F \rightarrow ( E )$

$F \rightarrow \text{id}$



# SLR Parse Table for Expression Grammar

Grammar:

1.  $E \rightarrow E + T$

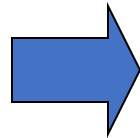
2.  $E \rightarrow T$

3.  $T \rightarrow T * F$

4.  $T \rightarrow F$

5.  $F \rightarrow ( E )$

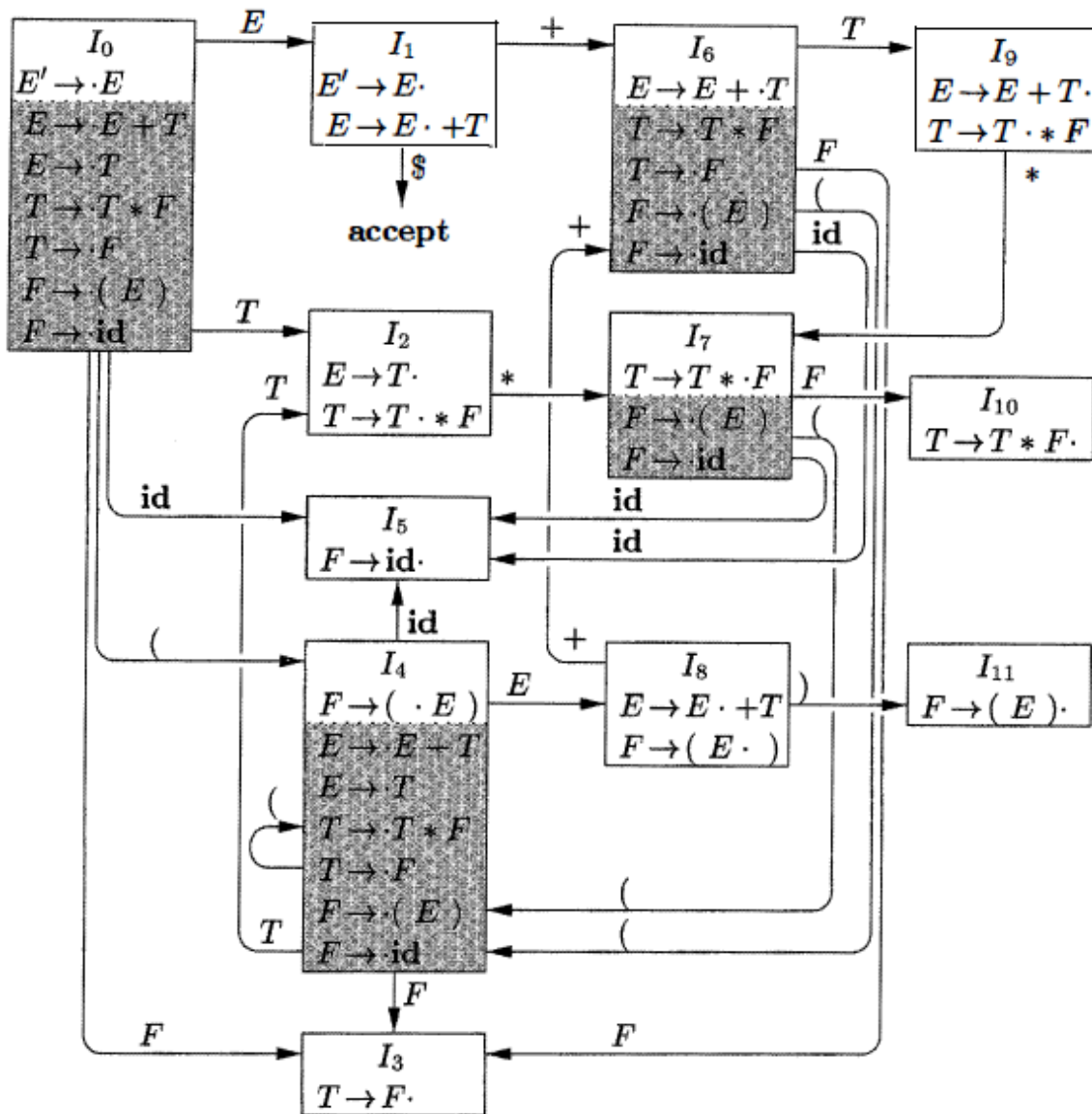
6.  $F \rightarrow \mathbf{id}$



Shift & goto 5

Reduce by  
production #1

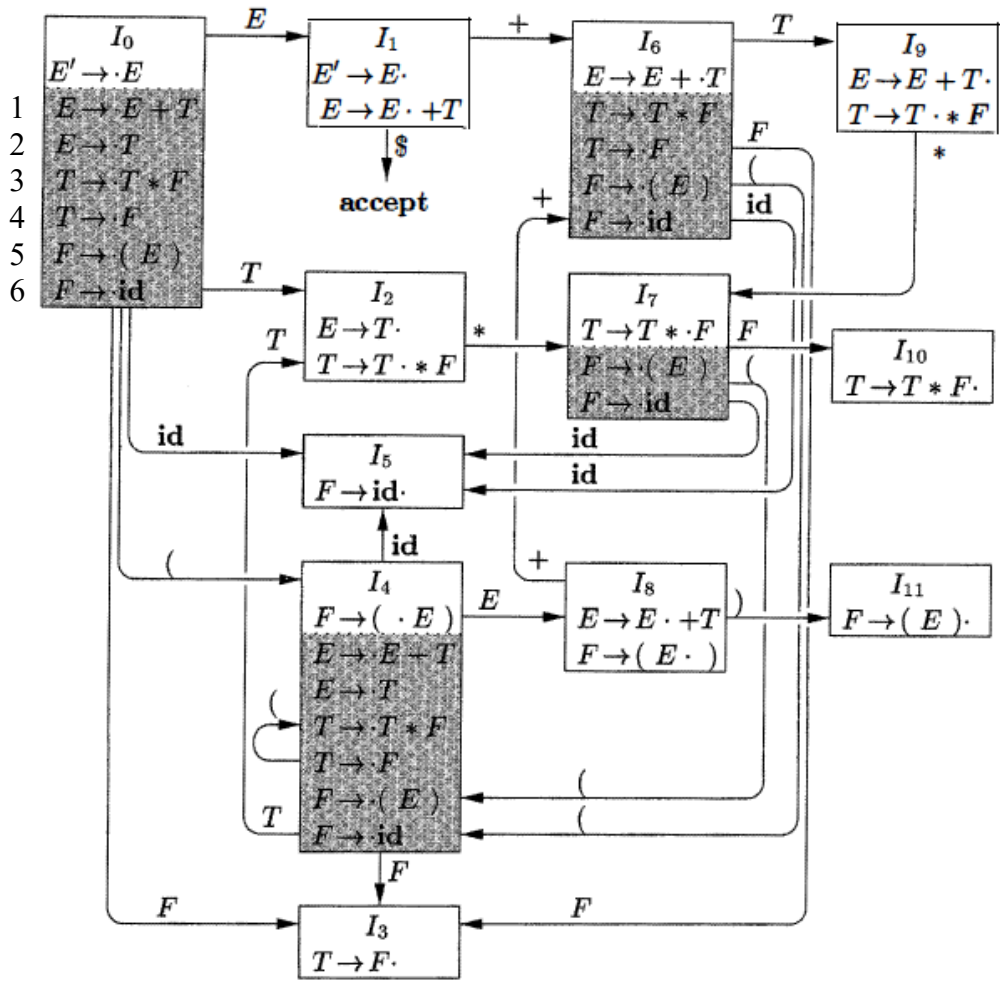
state	action						goto		
	id	+	*	(	)	\$	E	T	F
0	s5			s4			1	2	3
1		s6				acc			
2		r2	s7		r2	r2			
3		r4	r4		r4	r4			
4	s5			s4			8	2	3
5		r6	r6		r6	r6			
6	s5			s4				9	3
7	s5			s4					10
8		s6			s11				
9		r1	s7		r1	r1			
10		r3	r3		r3	r3			
11		r5	r5		r5	r5			



*goto*

<i>state</i>	<i>E</i>	<i>T</i>	<i>F</i>
0	1	2	3
1			
2			
3			
4	8	2	3
5			
6		9	3
7			10
8			
9			
10			
11			

$\text{FOLLOW}(E) = \{ + \} \$$   
 $\text{FOLLOW}(T) = \{ + * \} \$$   
 $\text{FOLLOW}(F) = \{ + * \} \$$



state	action				
	id	+	*	( )	\$
0	s5			s4	
1		s6			acc
2	r2		s7	r2	r2
3	r4		r4	r4	r4
4	s5			s4	
5	r6		r6	r6	r6
6	s5			s4	
7	s5			s4	
8		s6		s11	
9	r1		s7	r1	r1
10	r3		r3	r3	r3
11	r5		r5	r5	r5



# Moves of an SLR parser on $\text{id} * \text{id} + \text{id}$ Using the SLR Parse Table on Previous Slide

	STACK	SYMBOLS	INPUT	ACTION
(1)	0		<b>id * id + id \$</b>	shift
(2)	0 5	<b>id</b>	<b>* id + id \$</b>	reduce by $F \rightarrow \text{id}$
(3)	0 3	$F$	<b>* id + id \$</b>	reduce by $T \rightarrow F$
(4)	0 2	$T$	<b>* id + id \$</b>	shift
(5)	0 2 7	$T *$	<b>id + id \$</b>	shift
(6)	0 2 7 5	$T * \text{id}$	<b>+ id \$</b>	reduce by $F \rightarrow \text{id}$
(7)	0 2 7 10	$T * F$	<b>+ id \$</b>	reduce by $T \rightarrow T * F$
(8)	0 2	$T$	<b>+ id \$</b>	reduce by $E \rightarrow T$
(9)	0 1	$E$	<b>+ id \$</b>	shift
(10)	0 1 6	$E +$	<b>id \$</b>	shift
(11)	0 1 6 5	$E + \text{id}$	<b>\$</b>	reduce by $F \rightarrow \text{id}$
(12)	0 1 6 3	$E + F$	<b>\$</b>	reduce by $T \rightarrow F$
(13)	0 1 6 9	$E + T$	<b>\$</b>	reduce by $E \rightarrow E + T$
(14)	0 1	$E$	<b>\$</b>	accept

Moves of an SLR parser on  $id * id + id$   
Using the SLR Parse Table on Previous Slide

state	action					goto			
	id	+	*	(	)	\$	E	T	F
0	s5			s4			1	2	3
1		s6				acc			
2		r2	s7		r2	r2			
3		r4	r4		r4	r4			
4	s5			s4			8	2	3
5		r6	r6		r6	r6			
6	s5			s4				9	3
7	s5			s4					10
8		s6			s11				
9		r1	s7		r1	r1			
10		r3	r3		r3	r3			
11		r5	r5		r5	r5			

Grammar:

1.  $E \rightarrow E + T$
2.  $E \rightarrow T$
3.  $T \rightarrow T * F$
4.  $T \rightarrow F$
5.  $F \rightarrow ( E )$
6.  $F \rightarrow id$

	STACK	SYMBOLS	INPUT	ACTION
(1)	0		<b>id * id + id \$</b>	shift
(2)	0 5	<b>id</b>	<b>* id + id \$</b>	reduce by $F \rightarrow id$
(3)	0 3	<b>F</b>	<b>* id + id \$</b>	reduce by $T \rightarrow F$
(4)	0 2	<b>T</b>	<b>* id + id \$</b>	shift
(5)	0 2 7	<b>T *</b>	<b>id + id \$</b>	shift
(6)	0 2 7 5	<b>T * id</b>	<b>+ id \$</b>	reduce by $F \rightarrow id$
(7)	0 2 7 10	<b>T * F</b>	<b>+ id \$</b>	reduce by $T \rightarrow T * F$
(8)	0 2	<b>T</b>	<b>+ id \$</b>	reduce by $E \rightarrow T$
(9)	0 1	<b>E</b>	<b>+ id \$</b>	shift
(10)	0 1 6	<b>E +</b>	<b>id \$</b>	shift
(11)	0 1 6 5	<b>E + id</b>	<b>\$</b>	reduce by $F \rightarrow id$
(12)	0 1 6 3	<b>E + F</b>	<b>\$</b>	reduce by $T \rightarrow F$
(13)	0 1 6 9	<b>E + T</b>	<b>\$</b>	reduce by $E \rightarrow E + T$
(14)	0 1	<b>E</b>	<b>\$</b>	accept