

CS 4300: Compiler Theory

Chapter 5 Syntax-Directed Translation

Xuejun Liang

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Outlines (Sections)

1. Syntax-Directed Definitions
2. Evaluation Orders for SDD's
3. Applications of Syntax-Directed Definition
4. Syntax-Directed Translation Schemes
5. Implementing L-Attributed SDD's

1. Syntax-directed Definition

- A syntax-directed definition (SSD) specifies the values of attributes by associating semantic rules with the grammar productions

PRODUCTION	SEMANTIC RULE
$E \rightarrow E_1 + T$	$E.code = E_1.code \parallel T.code \parallel '+'$

- A syntax-directed translation scheme embeds program fragments called semantic actions within production bodies

$$E \rightarrow E_1 + T \{ \text{print } '+' \}$$

- Between the two notations
 - syntax-directed definitions can be more readable, and hence more useful for specifications.
 - However, translation schemes can be more efficient, and hence more useful for implementations

Attributes

- A synthesized attribute at node N is defined only in terms of attribute values at the children of N and at N itself.
- An inherited attribute at node N is defined only in terms of attribute values at N's parent , N itself, and N's siblings
- Attribute values typically represent
 - Numbers (literal constants)
 - Strings (literal constants)
 - Memory locations, such as a frame index of a local variable or function argument
 - A data type for type checking of expressions
 - Scoping information for local declarations
 - Intermediate program representations

Example Syntax-directed Definition

A simple desk calculator

Production	Semantic Rule
$L \rightarrow E \mathbf{n}$	$L.val = E.val$
$E \rightarrow E_1 + T$	$E.val = E_1.val + T.val$
$E \rightarrow T$	$E.val = T.val$
$T \rightarrow T_1 * F$	$T.val = T_1.val * F.val$
$T \rightarrow F$	$T.val = F.val$
$F \rightarrow (E)$	$F.val = E.val$
$F \rightarrow \mathbf{digit}$	$F.val = \mathbf{digit.lexval}$

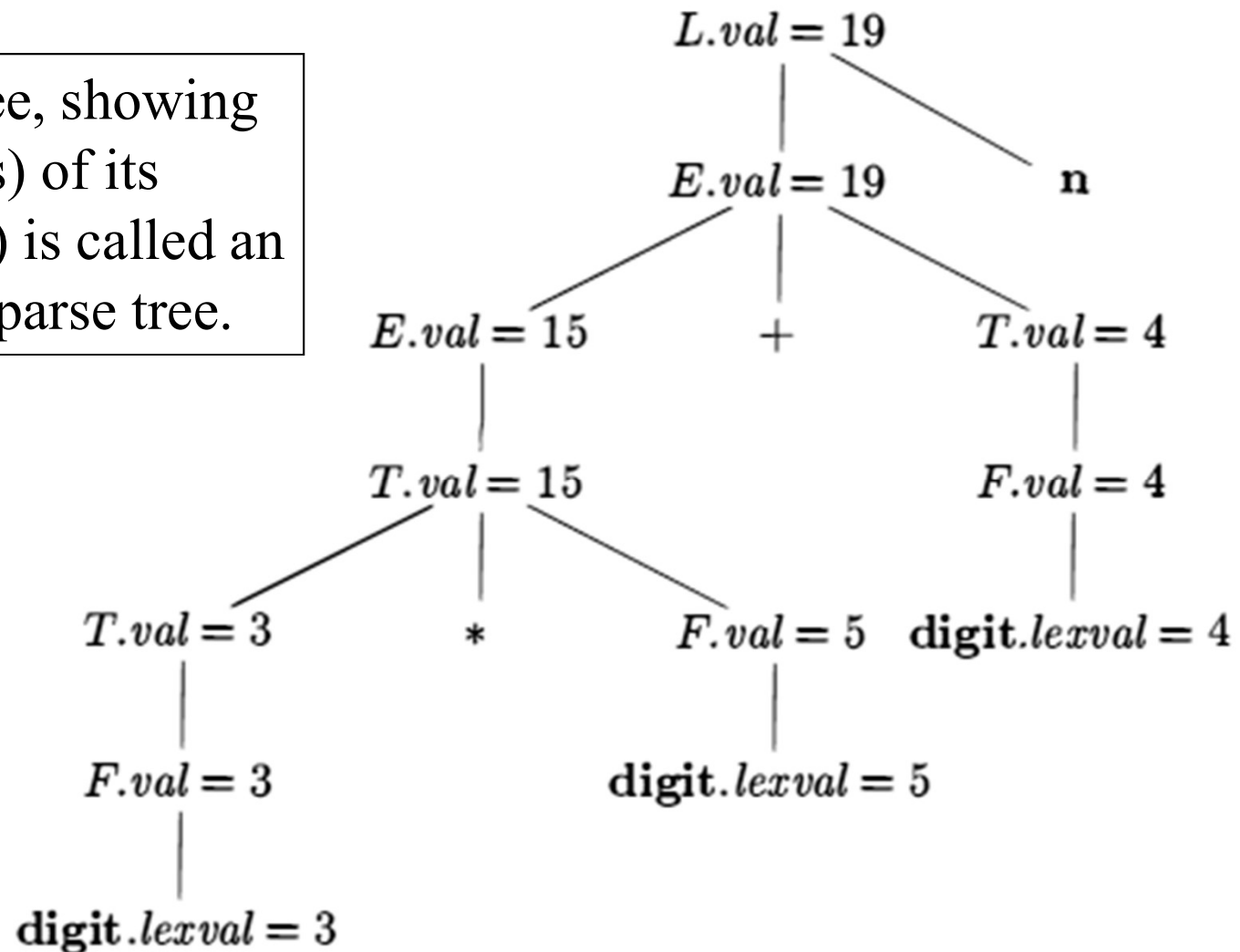
An SDD with only synthesized attributes is called S-attributed.

An SDD without side effects is called an attribute grammar

Note: all attributes in this example are of the synthesized type

Annotated Parse Tree for $3 * 5 + 4 n$

A parse tree, showing the value(s) of its attribute(s) is called an annotated parse tree.



Annotating a Parse Tree With Depth-First Traversals

With synthesized attributes, we can evaluate attributes in any bottom-up order, such as that of a postorder traversal of the parse tree.

```
procedure visit(n : node);  
begin  
  for each child m of n, from left to right do  
    visit(m);  
  evaluate semantic rules at node n  
end
```

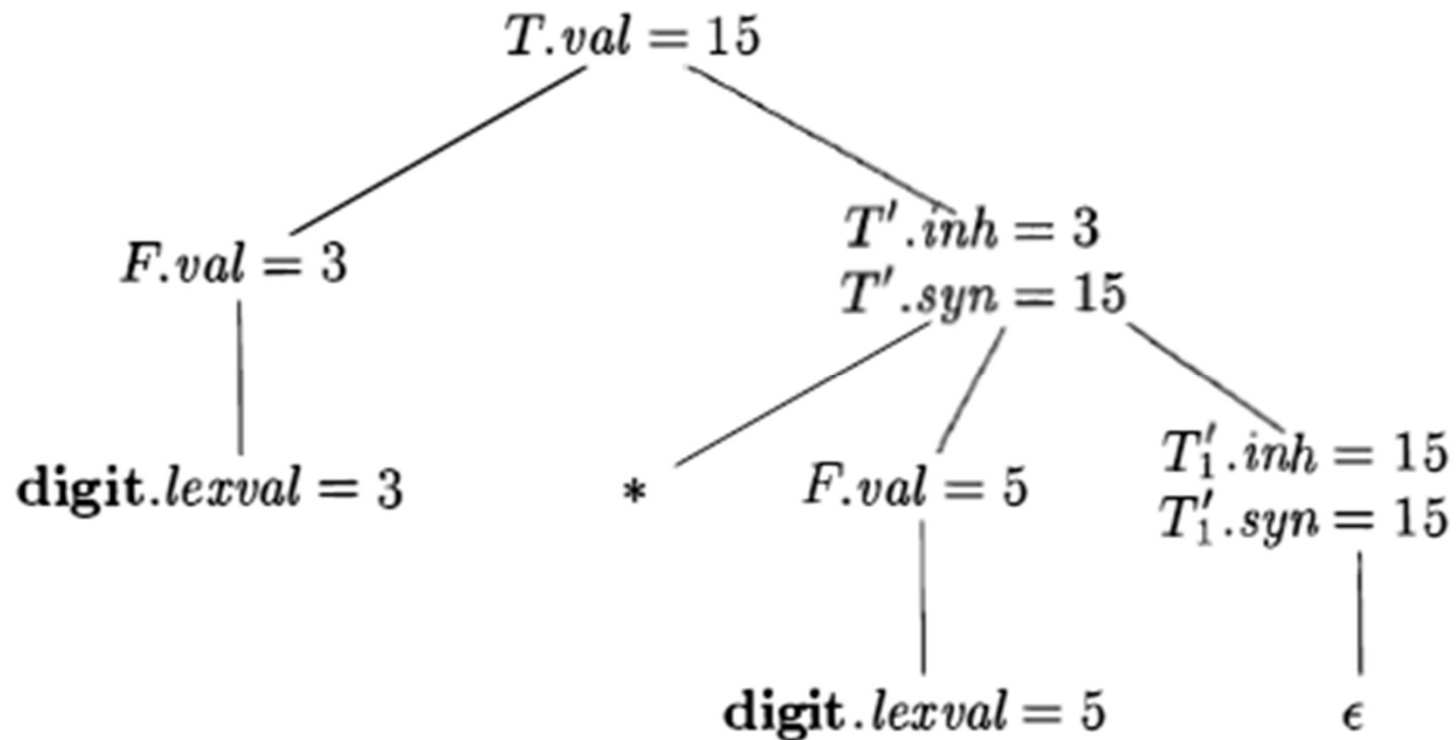
An SDD Based on a Grammar Suitable for Top-down Parsing

PRODUCTION	SEMANTIC RULES
1) $T \rightarrow F T'$	$T'.inh = F.val$ $T.val = T'.syn$
2) $T' \rightarrow * F T'_1$	$T'_1.inh = T'.inh \times F.val$ $T'.syn = T'_1.syn$
3) $T' \rightarrow \epsilon$	$T'.syn = T'.inh$
4) $F \rightarrow \mathbf{digit}$	$F.val = \mathbf{digit.lexval}$

$T \rightarrow T * F$ $T \rightarrow F$ $F \rightarrow \mathbf{digit}$
--

<p>An inherited attribute for nonterminal T' is used to pass the operand to the operator</p>

Annotated Parse Tree for $3 * 5$




An inherited attribute for nonterminal T' is used to pass the operand to the operator

Example Attribute Grammar with Synthesized & Inherited Attributes

Simple Type Declaration

Production	Semantic Rule
$D \rightarrow T L$	$L.inh = T.type$
$T \rightarrow \mathbf{int}$	$T.type = \text{'integer'}$
$T \rightarrow \mathbf{float}$	$T.type = \text{'float'}$
$L \rightarrow L_1, \mathbf{id}$	$L_1.inh = L.inh;$ $addtype(\mathbf{id}.entry, L.inh)$
$L \rightarrow \mathbf{id}$	$addtype(\mathbf{id}.entry, L.inh)$

treated as
dummy
synthesized
attribute



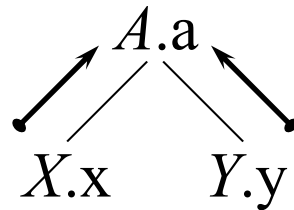
Synthesized: $T.type, \mathbf{id}.entry$

Inherited: $L.inh$

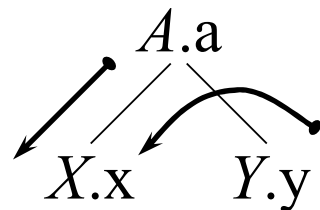
2. Evaluation Orders for SDD 's

A dependency graph depicts the flow of information among the attribute instances in a particular parse tree

$A \rightarrow XY$



$$A.a = f(X.x, Y.y)$$

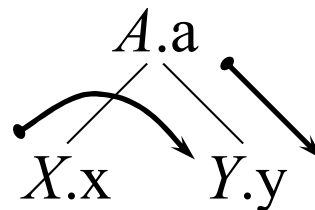


$$X.x = f(A.a, Y.y)$$

Direction of



value dependence

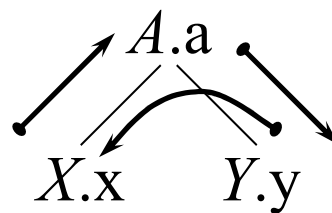


$$Y.y = f(A.a, X.x)$$

Evaluation Orders for SDD 's (Cont.)

- Edges in the dependency graph determine the evaluation order for attribute values
 - Dependency graphs cannot be cyclic
- So, dependency graph is a directed acyclic graph (DAG)

$A \rightarrow X Y$



$A.a := f(X.x)$

$X.x := f(Y.y)$

$Y.y := f(A.a)$

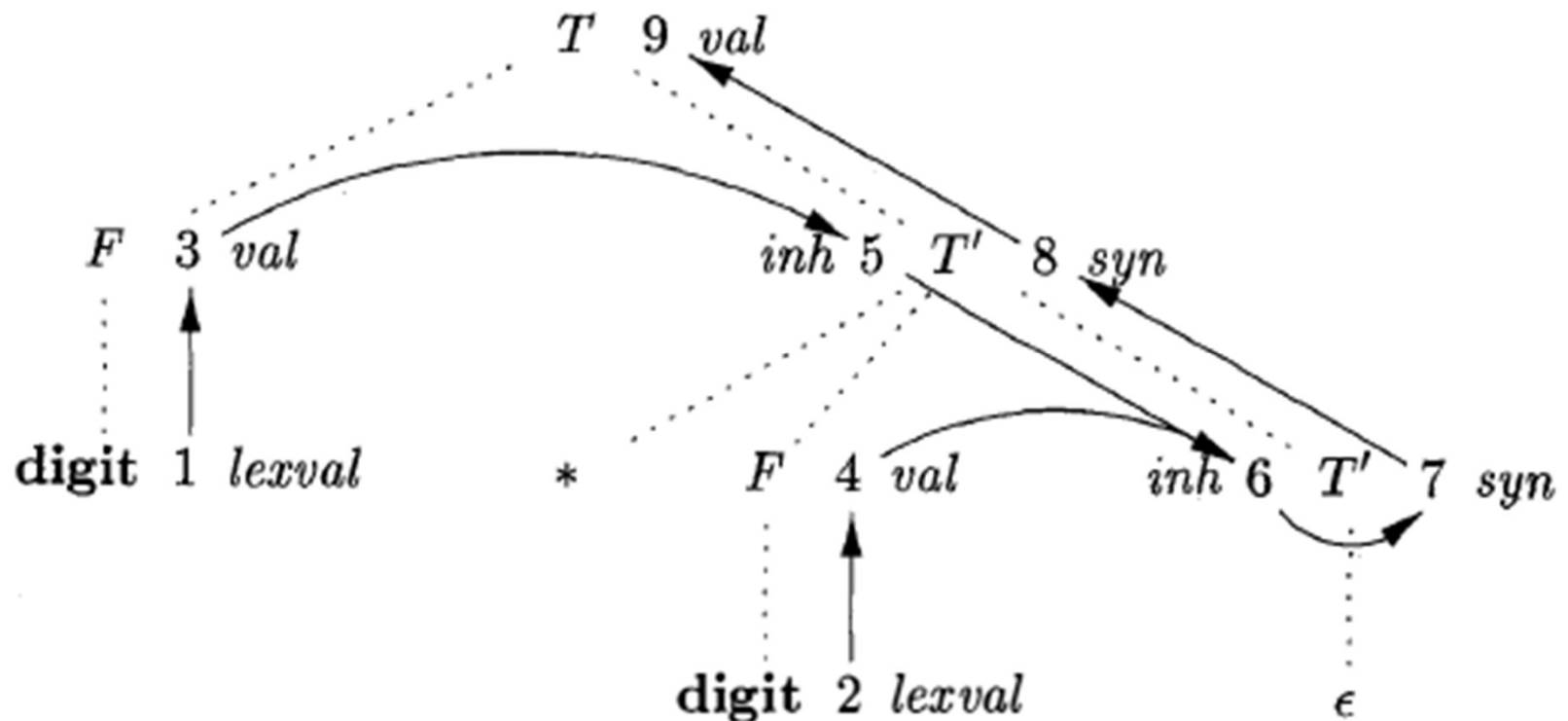
Direction of



value dependence

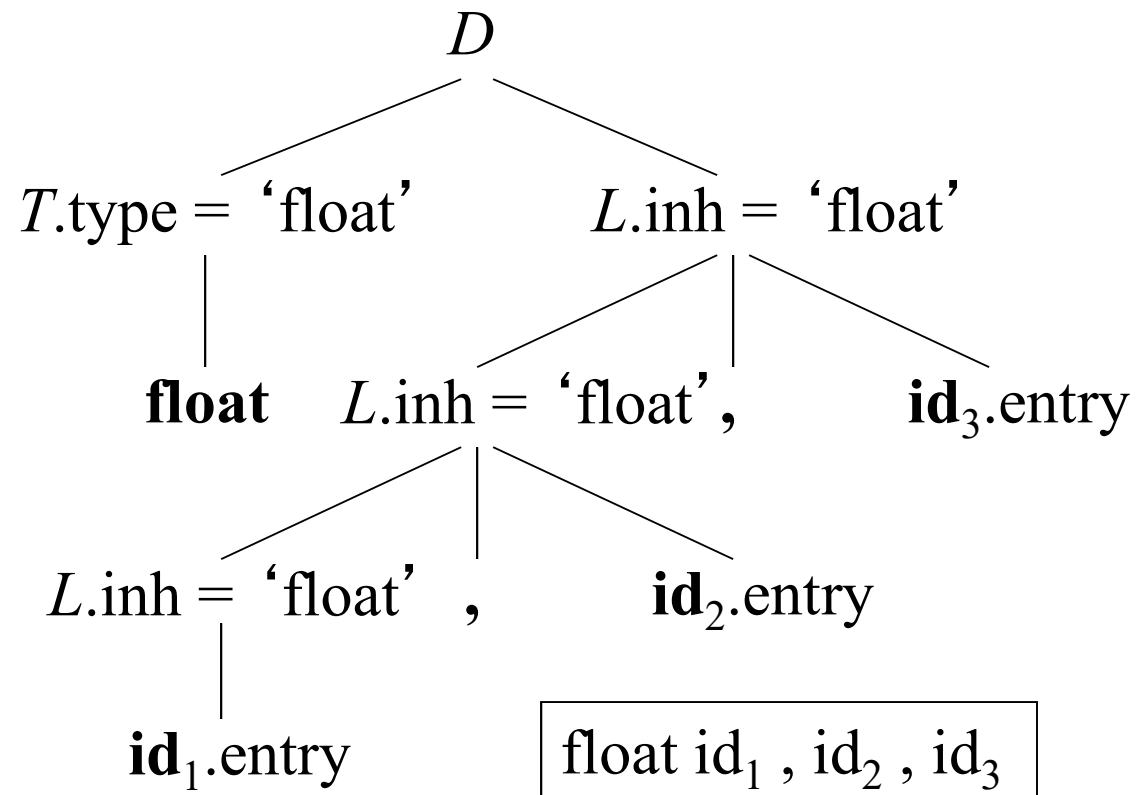
Error: cyclic dependence

Example Annotated Parse Tree with Dependency Graph

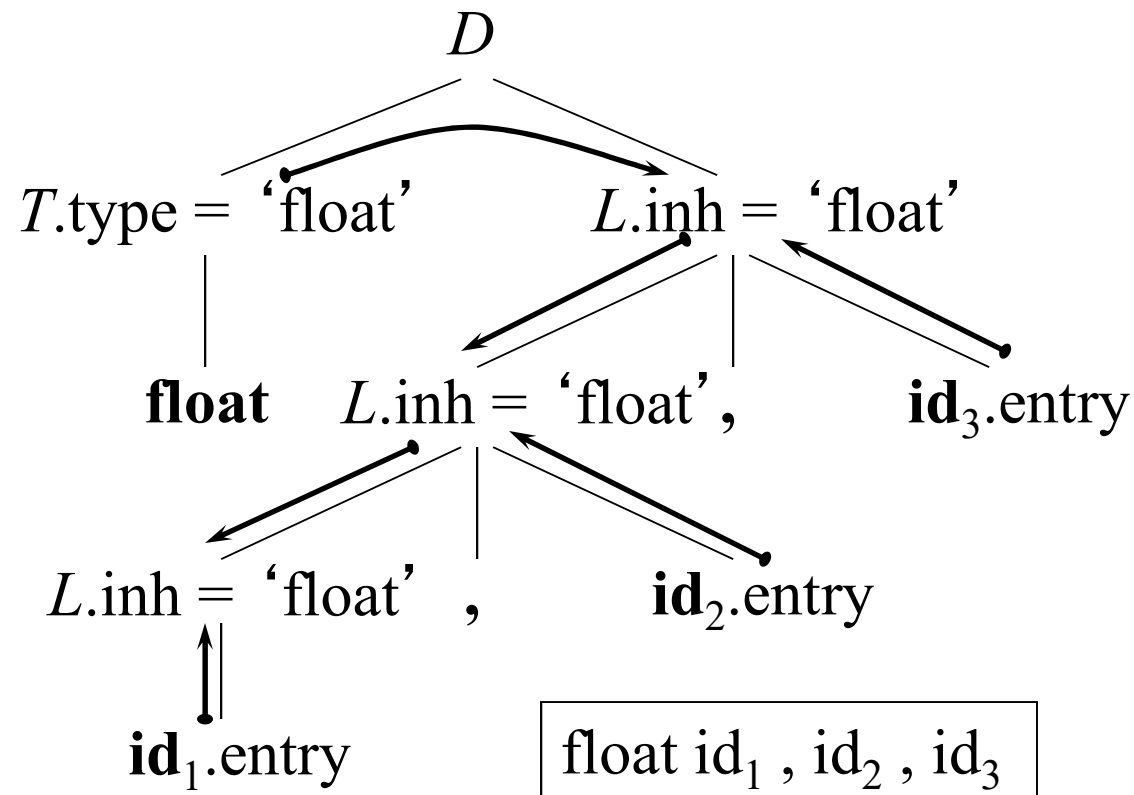


$3 * 5$

Example Annotated Parse Tree



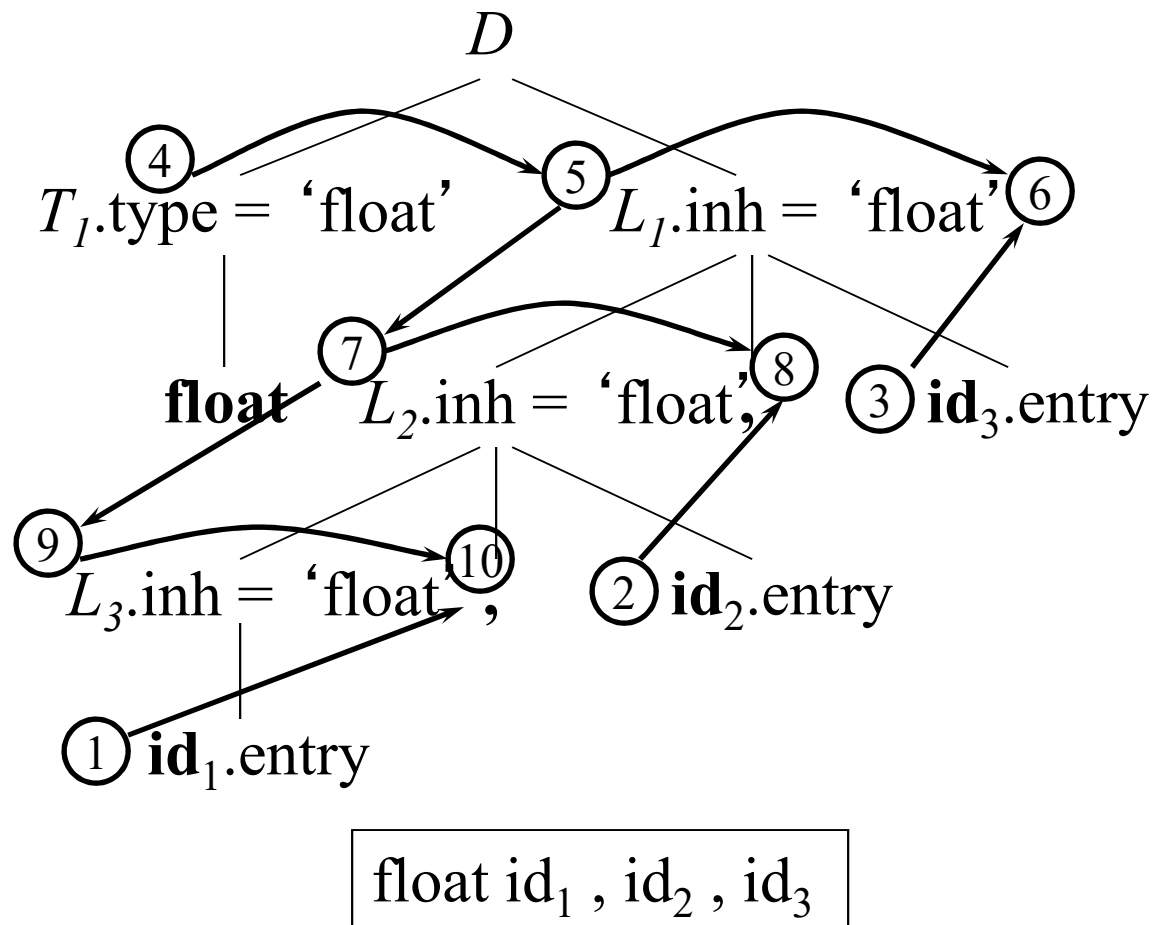
Example Annotated Parse Tree with Dependency Graph



Evaluation Order

- A **topological sort** of a directed acyclic graph (DAG) is any ordering m_1, m_2, \dots, m_n of the nodes of the graph, such that if $m_i \rightarrow m_j$ is an edge, then m_i appears before m_j
- Any topological sort of a dependency graph gives a valid evaluation order of the semantic rules
- Example: Topological orders of DAG on slide 13
 - 1, 2, 3, 4, 5, 6, 7, 8, 9.
 - 1, 3, 5, 2, 4, 6, 7, 8, 9.

Example Parse Tree with Topologically Sorted Actions



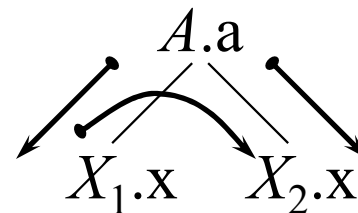
Topological sort:

1. Get $\text{id}_1.entry$
2. Get $\text{id}_2.entry$
3. Get $\text{id}_3.entry$
4. $T_1.type = \text{'float'}$
5. $L_1.inh = T_1.type$
6. $addtype(\text{id}_3.entry, L_1.inh)$
7. $L_2.inh = L_1.inh$
8. $addtype(\text{id}_2.entry, L_2.inh)$
9. $L_3.inh = L_2.inh$
10. $addtype(\text{id}_1.entry, L_3.inh)$

L-Attributed Definitions

- A syntax-directed definition is **L-attributed** if each inherited attribute of X_j on the right side of production $A \rightarrow X_1 X_2 \dots X_n$ depends only on
 1. the attributes of the symbols X_1, X_2, \dots, X_{j-1}
 2. the inherited attributes of A

Shown: dependences
of inherited attributes



- L-attributed definitions allow for a natural order of evaluating attributes: **depth-first and left to right**
- Note: every S-attributed syntax-directed definition is also L-attributed

3. Applications of SDD

Construction of Syntax Trees

S-attributed Definition for Simple Expressions

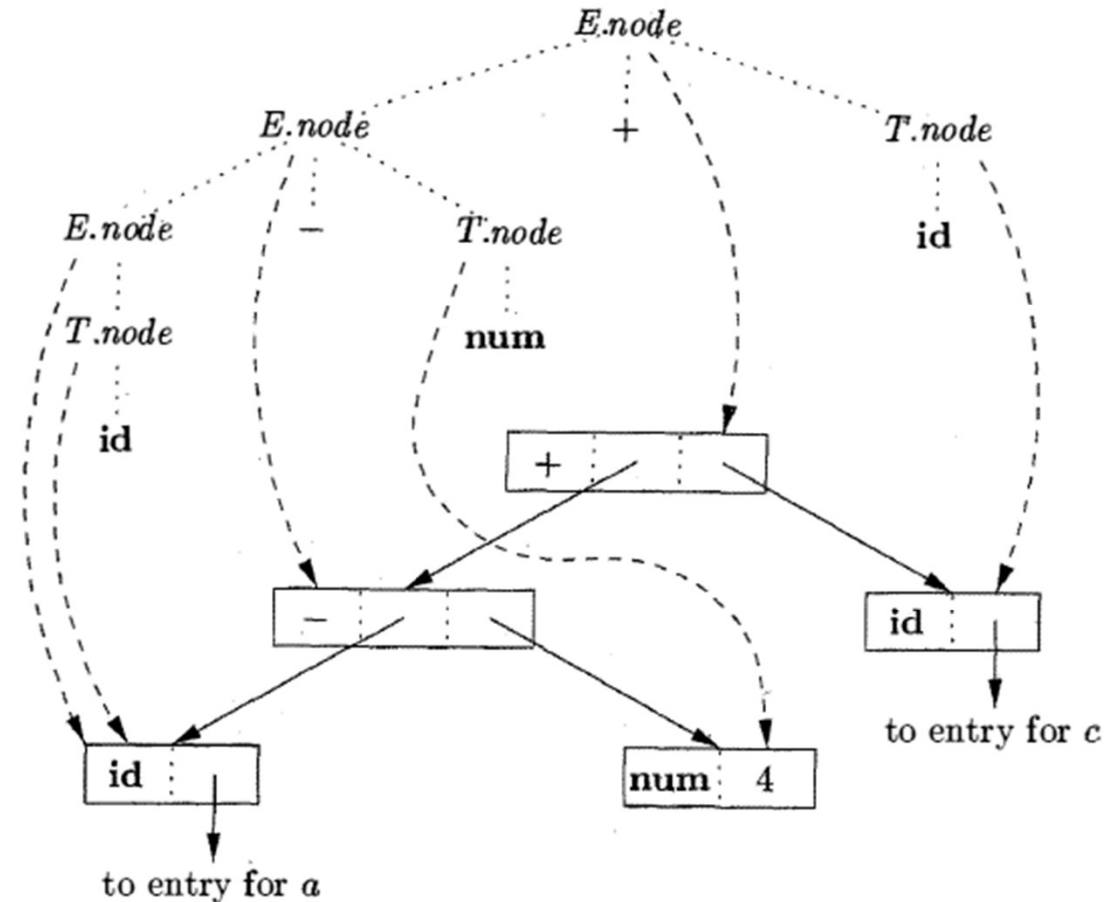
PRODUCTION	SEMANTIC RULES
1) $E \rightarrow E_1 + T$	$E.node = \mathbf{new} \text{ Node}(' + ', E_1.node, T.node)$
2) $E \rightarrow E_1 - T$	$E.node = \mathbf{new} \text{ Node}(' - ', E_1.node, T.node)$
3) $E \rightarrow T$	$E.node = T.node$
4) $T \rightarrow (E)$	$T.node = E.node$
5) $T \rightarrow \mathbf{id}$	$T.node = \mathbf{new} \text{ Leaf}(\mathbf{id}, \mathbf{id.entry})$
6) $T \rightarrow \mathbf{num}$	$T.node = \mathbf{new} \text{ Leaf}(\mathbf{num}, \mathbf{num.val})$

Note: This is a S-attributed definition, then
can be done during bottom-up parsing

Example: Syntax Tree for $a - 4 + c$

Steps in the construction
of the syntax tree

- 1) $p_1 = \text{new Leaf}(\text{id}, \text{entry-}a);$
- 2) $p_2 = \text{new Leaf}(\text{num}, 4);$
- 3) $p_3 = \text{new Node}('-', p_1, p_2);$
- 4) $p_4 = \text{new Leaf}(\text{id}, \text{entry-}c);$
- 5) $p_5 = \text{new Node}('+', p_3, p_4);$

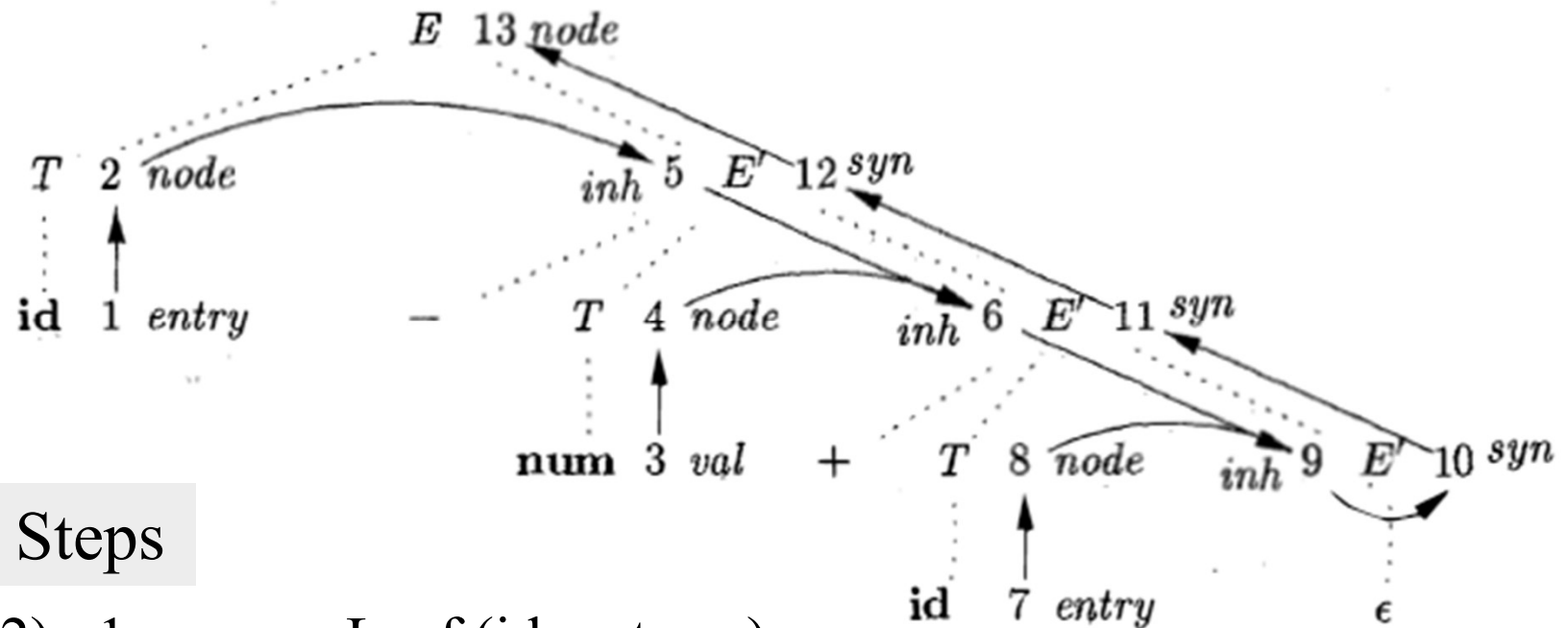


Constructing Syntax Tree During Top-Down Parsing

L-attributed Definition for Simple Expression

PRODUCTION	SEMANTIC RULES
1) $E \rightarrow T E'$	$E.node = E'.syn$ $E'.inh = T.node$
2) $E' \rightarrow + T E'_1$	$E'_1.inh = \mathbf{new Node}('+', E'.inh, T.node)$ $E'.syn = E'_1.syn$
3) $E' \rightarrow - T E'_1$	$E'_1.inh = \mathbf{new Node}('-', E'.inh, T.node)$ $E'.syn = E'_1.syn$
4) $E' \rightarrow \epsilon$	$E'.syn = E'.inh$
5) $T \rightarrow (E)$	$T.node = E.node$
6) $T \rightarrow \mathbf{id}$	$T.node = \mathbf{new Leaf}(\mathbf{id}, \mathbf{id.entry})$
7) $T \rightarrow \mathbf{num}$	$T.node = \mathbf{new Leaf}(\mathbf{num}, \mathbf{num.val})$

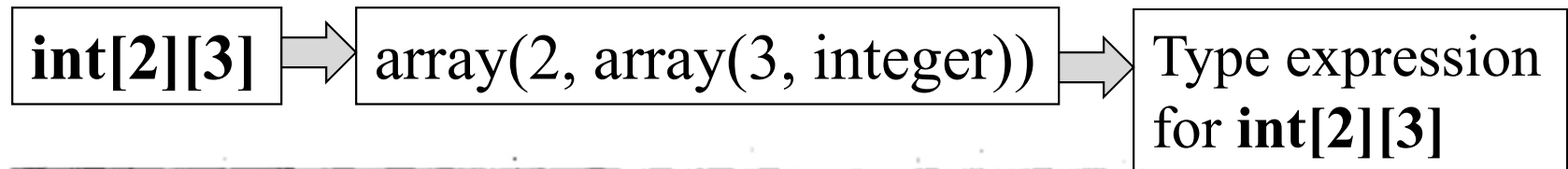
Example: Dependency Graph for a-4+c



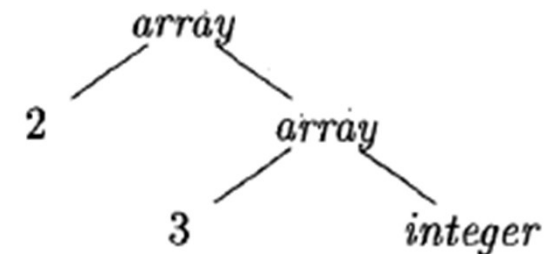
Steps

- 2) $p1 == \text{new Leaf}(id, \text{entry-a}) ;$
- 4) $p2 == \text{new Leaf}(num, 4) ;$
- 6) $p3 == \text{new Node}('-', p1, p2) ;$
- 8) $p4 == \text{new Leaf}(id, \text{entry-c}) ;$
- 9) $p5 == \text{new Node}('+', p3, p4) ;$

The Structure of a Type



PRODUCTION	SEMANTIC RULES
$T \rightarrow B C$	$T.t = C.t$ $C.b = B.t$
$B \rightarrow \text{int}$	$B.t = \text{integer}$
$B \rightarrow \text{float}$	$B.t = \text{float}$
$C \rightarrow [\text{num}] C_1$	$C.t = \text{array}(\text{num.val}, C_1.t)$ $C_1.b = C.b$
$C \rightarrow \epsilon$	$C.t = C.b$



T generates either a basic type or an array type

Annotated Parse Tree for `int[2][3]`

