

# Math 2300, Spring 2020

## Proofs using the Principle of Mathematical Induction

### **Principle of Mathematical Induction** (Epp, p. 246)

Let  $P(n)$  be a property that is defined for integers  $n$ , and let  $a$  be a fixed integer. Suppose the following two statements are true:

1.  $P(a)$  is true.
2. For all integers  $k \geq a$ , if  $P(k)$  is true then  $P(k + 1)$  is true.

Then the statement

for all integers  $n \geq a$ ,  $P(n)$

is true.

Dr. Martin's 5 step method to prove  $P(n)$  for all integers  $n \geq n_0$ .

#### **1. Base Case: $P(n_0)$**

If it is an equation be sure to check both sides separately.

#### **2. Write down the Induction Hypothesis: $n=k$**

Where  $k$  is a particular, but arbitrary integer greater than or equal to  $n_0$

**Let  $k \in \mathbb{Z} \ni k \geq n_0$  and suppose  $P(k)$**

#### **3. Write down what needs to be proved: $n = k + 1$**

**We must show that  $P(k+1)$**

#### **4. Show $P(k)$ implies $P(k+1)$ by clear and convincing argument, usually starts:**

**Consider  $P(k+1)$**

#### **5. Conclusion**

**By PMI  $P(n) \forall n \in \mathbb{Z} \ni n \geq n_0$**