

Math 1600, Section 5, Fall 2015 – Statistics  
HW 13 – Due December 10, 2015

Name: \_\_\_\_\_

True or False:

1. Confidence intervals based on the  $t$ -distribution are wider than those based on the standard normal distribution.

T or F

2. A hypothesis test for a sample mean with small samples and sample size of  $n$  has  $n/2$  degrees of freedom.

T or F

3. The  $t$ -distribution has less variability than the standard normal distribution.

T or F

Short Answer:

4. The quantity  $T = \frac{\bar{X} - \mu}{S/\sqrt{n}}$  has \_\_\_\_\_ degrees of freedom.

5. The  $t$ -distribution is symmetric about \_\_\_\_\_.

6. The upper .01 point of the  $t$ -distribution with 14 d.f. is \_\_\_\_\_.

7. The lower .05 point of the  $t$ -distribution with 7 d.f. is \_\_\_\_\_.

8. The 97.5th percentile of the  $t$ -distribution with 23 d.f. is \_\_\_\_\_.

9. For the  $t$ -distribution with 11 d.f. the probability  $T > 2.9$  is between \_\_\_\_\_ and \_\_\_\_\_.

Computations:

10. Given the following, compute a 95% confidence interval for the population mean,  $\mu$ .

$$n = 17, \sum x_i = 220, \sum (x_i - \bar{x})^2 = 75$$

11. A manager wants to estimate the time it takes to process an order. A random sample of 6 recent orders yields the following times:

28 26 25 30 22 34

Determine a 90% confidence interval for the true time to fill orders. State any assumptions you make.

**True or False:**

1. The  $\chi^2$  distribution is an example of a symmetric distribution.

T or F

2. Inferences on a population standard deviation are based on the  $t$ -distribution.

T or F

3. If a 95% confidence interval contains a particular value,  $\mu_0$ , then the two sided hypothesis test with a null hypothesis using  $\mu_0$  with  $\alpha = .05$  would lead to a rejection of the null hypothesis.

T or F

**Short Answer:**

4. The upper 5% of the  $\chi^2$  distribution with 8 degrees of freedom is \_\_\_\_\_.

5. 30.19 is the upper \_\_\_\_\_% of the  $\chi^2$  with 17 degrees of freedom.

6. The lower 5% of the  $\chi^2$  distribution with 22 degrees of freedom is \_\_\_\_\_.

**(For 7 and 8.)** Suppose that from a random sample a 90% confidence interval for the population mean has been found to be (12.8, 14.3).

7. Would  $H_0 : \mu = 15$  be rejected in favor of  $H_1 : \mu \neq 15$  at  $\alpha = .10$ ?

a) yes

b) no

c) cannot tell

8. Would  $H_0 : \mu = 13$  be rejected in favor of  $H_1 : \mu \neq 13$  at  $\alpha = .10$ ?

a) yes

b) no

c) cannot tell

**Computations:**

9. For data from a set of  $n=10$  observations, one has calculated the 95% confidence interval for  $\sigma$  and obtained the result (4.05, 10.75).

a. What was the standard deviation  $s$  for the sample? (Hint: Examine how  $s$  enters the formula of a confidence interval.)

b. Calculate a 90% confidence interval for  $\sigma$ .