Logic

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Based on slides from http://aima.eecs.berkeley.edu/2nd-ed/slides-ppt/

Outline

- · Knowledge-based agents
- · Wumpus world
- Logic in general models and entailment
- Propositional (Boolean) logic
- Equivalence, validity, satisfiability
- Inference rules and theorem proving
 - forward chaining
 - backward chaining
 - resolution

Knowledge bases

domain-independent algorithms Knowledge base domain-specific content

- Knowledge base = set of sentences in a formal language
- Declarative approach to building an agent (or other system):

 Tell it what it needs to know
- Then it can ${\tt As\,k}$ itself what to do answers should follow from the KB
- Agents can be viewed at the knowledge level i.e., what they know, regardless of how implemented
- - Or at the implementation level

 i.e., data structures in KB and algorithms that manipulate them

A simple knowledge-based agent

function KB-AGENT(percept) returns an action static: KB, a knowledge base

t, a counter, initially 0, indicating time

Tell(KB, Make-Percept-Sentence(percept, t)) $action \leftarrow Ask(KB, Make-Action-Query(t))$ Tell(KB, Make-Action-Sentence(action, t))

 $t \leftarrow t + 1$ return action

The agent must be able to:

Represent states, actions, etc.

Incorporate new percepts
Update internal representations of the world

Deduce hidden properties of the world

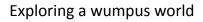
Deduce appropriate actions

Wumpus World PEAS description

- - gold +1000, death -1000
 - -1 per step, -10 for using the arrow
- - Squares adjacent to wumpus are smelly
 - Squares adjacent to pit are breezy
 Glitter iff gold is in the same square
 - Shooting kills wumpus if you are facing it - Shooting uses up the only arrow
 - Grabbing picks up gold if in same square
 - Releasing drops the gold in same square
- SE SESS \$5,555 §
- Sensors: Stench, Breeze, Glitter, Bump, Scream
- Actuators: Left turn, Right turn, Forward, Grab, Release, Shoot

Wumpus world characterization

- Fully Observable No only local perception
- <u>Deterministic</u> Yes outcomes exactly specified
- Episodic No sequential at the level of actions
- Static Yes Wumpus and Pits do not move
- <u>Discrete</u> Yes
- Single-agent? Yes Wumpus is essentially a natural feature





Exploring a wumpus world



Exploring a wumpus world



Exploring a wumpus world



Exploring a wumpus world



Exploring a wumpus world



Exploring a wumpus world



Exploring a wumpus world



Logic in general

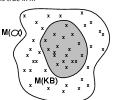
- Logics are formal languages for representing information such that conclusions can be drawn
- Semantics define the "meaning" of sentences;
 i.e., define truth of a sentence in a world
- ♦ E.g., the language of arithmetic
 - $x+2 \ge y$ is a sentence; $x2+y > \{\}$ is not a sentence
 - $x+2 \ge y$ is true iff the number x+2 is no less than the number y
 - x+2 ≥ y is true in a world where x = 7, y = 1
 x+2 ≥ y is false in a world where x = 0, y = 6

- Entailment
 - Entailment means that one thing follows from another:

- Knowledge base \textit{KB} entails sentence α if and only if α is true in all worlds where KB is true
 - E.g., the KB containing "the Giants won" and "the Reds won" entails "Either the Giants won or the Reds won"
 - E.g., x+y = 4 entails 4 = x+y
 - Entailment is a relationship between sentences (i.e., syntax) that is based on semantics

Models

- Logicians typically think in terms of models, which are formally structured worlds with respect to which truth can be evaluated
- $M(\alpha)$ is the set of all models of α
- Then KB $\models \alpha$ iff $M(KB) \subseteq M(\alpha)$
 - E.g. KB = Giants won and Reds won α = Giants won



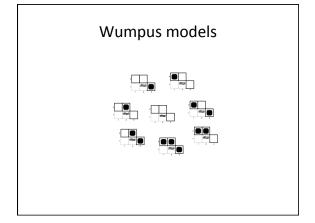
Entailment in the wumpus world

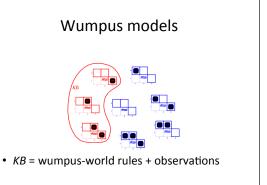
Situation after detecting nothing in [1,1], moving right, breeze in

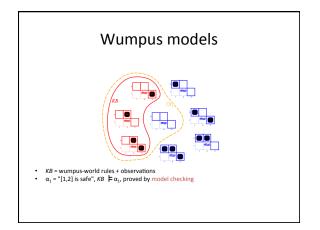
Consider possible models for KB assuming only pits

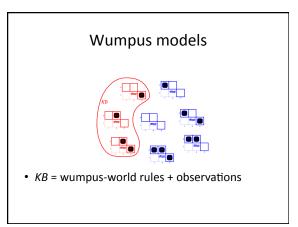
3 Boolean choices ⇒ 8 possible

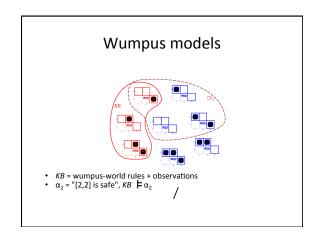
?	?		
A	B	?	











Inference • KB ⊢_i α = sentence α can be derived from KB by procedure i • Soundness: i is sound if whenever KB ⊢_i α, it is also true that KB ⊨ α • Completeness: i is complete if whenever KB ⊨ α, it is also true that KB ⊢_i α • Preview: we will define a logic (first-order logic) which is expressive enough to say almost anything of interest, and for which there exists a sound and complete inference procedure. • That is, the procedure will answer any question whose answer follows from what is known by the KB.

Propositional logic: Syntax

- Propositional logic is the simplest logic illustrates basic ideas
- The proposition symbols P₁, P₂ etc are sentences
 - If S is a sentence, ¬S is a sentence (negation)
 - If S₁ and S₂ are sentences, S₁ \wedge S₂ is a sentence (conjunction)
 - If S₁ and S₂ are sentences, S₁ v S₂ is a sentence (disjunction)
 - If S_1 and S_2 are sentences, $S_1 \Rightarrow S_2$ is a sentence (implication)
 - $\ \ \mbox{If S}_1 \mbox{ and S}_2 \mbox{ are sentences, S}_1 \Leftrightarrow \mbox{S}_2 \mbox{ is a sentence (biconditional)}$

Propositional logic: Semantics

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Each model specifies true/false for each proposition symbol
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\begin{array}{ccc} \text{E.g. P}_{1,2} & \text{P}_{2,2} & \text{P}_{3,1} \\ \text{false} & \text{true} & \text{false} \end{array}
```

With these symbols, 8 possible models, can be enumerated automatically.

Rules for evaluating truth with respect to a model m:

Simple recursive process evaluates an arbitrary sentence, e.g.,

 $\neg \, \mathsf{P}_{1,2} \, \wedge \, (\mathsf{P}_{2,2} \vee \mathsf{P}_{3,1}) = true \, \wedge \, (true \vee false) = \, true \, \wedge \, true = true$

Truth tables for connectives

P	Q	$\neg P$	$P \wedge Q$	$P \lor Q$	$P \Rightarrow Q$	$P \Leftrightarrow Q$
false	false	true	false	false	true	true
false	true	true	false	true	true	false
true	false	false	false	true	false	false
true	true	false	true	true	true	true

Wumpus world sentences

Let $P_{i,j}$ be true if there is a pit in [i,j]. Let $B_{i,j}$ be true if there is a breeze in [i,j].

$$\begin{array}{lll} \text{R1:} & -\textbf{P}_{1,1} & \text{no pit in [1,1] always true} \\ \text{R4:} & -\textbf{B}_{1,1} & \text{no breeze in [1,1] based on percept} \\ \text{R5:} & \textbf{B}_{2,1} & \text{breeze in [2,1] based on percept} \end{array}$$

· "Pits cause breezes in adjacent squares"

$$\begin{array}{lll} \text{R2: } B_{1,1} \Leftrightarrow & (P_{1,2} \vee P_{2,1}) \text{ true in any WW} \\ \text{R3: } B_{2,1} \Leftrightarrow & (P_{1,1} \vee P_{2,2} \vee P_{3,1}) \text{ true in any WW} \end{array}$$

KB: R1^R2^R3^r4^r5

Truth tables for inference

$B_{1,1}$	$B_{2,1}$	$P_{1,1}$	$P_{1,2}$	$P_{2,1}$	$P_{2,2}$	$P_{3,1}$	R_1	R_2	R_3	R_4	R_5	KB
false	true	true	true	true	false	false						
false	false	false	false	false	false	true	true	true	false	true	false	false
1	1		1	1	1	1	:	1	1		:	1
false	true	false	false	false	false	false	true	true	false	true	true	false
false	true	false	false	false	false	true	true	true	true	true	true	true
false	true	false	false	false	true	false	true	true	true	true	true	true
false	true	false	false	false	true	true	true	true	true	true	true	true
false	true	false	false	true	false	false	true	false	false	true	true	false
1	1	1	1	1	1		- :	1	1		1	:
true	false	true	true	false	true	false						

Enumerate rows (different assignments to symbols),

if KB is true in row, check that α is too

Inference by enumeration

Depth-first enumeration of all models is sound and complete

function TT-Entails? (KB, α) returns true or false $symbols \leftarrow \text{a list of the proposition symbols in } KB \text{ and } \alpha$ $\textbf{return } \text{TT-Check-All}(KB, \alpha, symbols, [])$

function TT-CHECK-ALL(KB, α , symbols, model) returns true or false if EMPTY?(symbols) then if PL-TRUE?(KB, model) then return PL-TRUE?(α , model) else return true else do $P \leftarrow \text{FIRST}(symbols)$: $rst \leftarrow \text{REST}(symbols)$ return TT-CHECK-ALL(KB, α , rst, EXTEND(P, true, model) and TT-CHECK-ALL(KB, α , rst, EXTEND(P, false, model)

• For n symbols, time complexity is $O(2^n)$, space complexity is O(n)

Logical equivalence

• Two sentences are logically equivalent iff true in same models: $\alpha \equiv \beta$ iff $\alpha \models \beta$ and $\beta \models \alpha$

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(\alpha \wedge \beta) \equiv (\beta \wedge \alpha) commutativity of \wedge
                                                                    (\alpha \lor \beta) \equiv (\beta \lor \alpha) commutativity of \lor
 \begin{array}{c} (\alpha\vee\beta)\equiv(\beta\vee\alpha)\;\; {\rm commutativity}\;{\rm of}\;\vee\\ ((\alpha\wedge\beta)\wedge\gamma)\equiv(\alpha\wedge(\beta\wedge\gamma))\;\; {\rm associativity}\;{\rm of}\;\wedge\\ ((\alpha\vee\beta)\vee\gamma)\equiv(\alpha\vee(\beta\vee\gamma))\;\; {\rm associativity}\;{\rm of}\;\vee\\ \neg(\neg\alpha)\equiv\alpha\;\; {\rm double-negation}\; {\rm elimination}\\ (\alpha\Rightarrow\beta)\equiv(\neg\beta\Rightarrow\neg\alpha)\;\; {\rm contraposition}\\ (\alpha\Rightarrow\beta)\equiv(\neg\alpha\vee\beta)\;\; {\rm implication}\; {\rm elimination}\\ (\alpha\Rightarrow\beta)\equiv((\alpha\Rightarrow\beta)\wedge(\beta\Rightarrow\alpha))\;\; {\rm biconditional}\; {\rm elimination}\\ \neg(\alpha\wedge\beta)\equiv(\neg\alpha\vee\neg\beta)\;\; {\rm de}\; {\rm Morgan}\\ \neg(\alpha\vee\beta)\equiv(\neg\alpha\wedge\neg\beta)\;\; {\rm de}\; {\rm Morgan}\\ (\alpha\wedge(\beta\vee\gamma))\equiv((\alpha\wedge\beta)\vee(\alpha\wedge\gamma))\;\; {\rm distributivity}\; {\rm of}\;\wedge {\rm over}\;\vee\\ (\alpha\vee(\beta\wedge\gamma))\equiv((\alpha\vee\beta)\wedge(\alpha\vee\gamma))\;\; {\rm distributivity}\; {\rm of}\;\wedge {\rm over}\;\vee\\ (\alpha\vee(\beta\wedge\gamma))\equiv((\alpha\vee\beta)\wedge(\alpha\vee\gamma))\;\; {\rm distributivity}\; {\rm of}\;\vee {\rm over}\;\wedge\\ \end{array}
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Validity and satisfiability

A sentence is valid if it is true in all models, e.g., True, $A \lor \neg A$, $A \Rightarrow A$, $(A \land (A \Rightarrow B)) \Rightarrow B$

Validity is connected to inference via the Deduction Theorem: $\mathit{KB} \not\models \alpha$ if and only if $(\mathit{KB} \Rightarrow \alpha)$ is valid

A sentence is satisfiable if it is true in some model e.g., Av B, C

A sentence is unsatisfiable if it is true in no models e.g., $A \land \neg A$

Satisfiability is connected to inference via the following: $\mathit{KB} \models \alpha$ if and only if $(\mathit{KB} \land \neg \alpha)$ is unsatisfiable

Proof methods

- Proof methods divide into (roughly) two kinds:
 - Application of inference rules
 - Legitimate (sound) generation of new sentences from old
 - Proof = a sequence of inference rule applications
 Can use inference rules as operators in a standard search algorithm
 - Typically require transformation of sentences into a normal form

 - Model checking

 truth table enumeration (always exponential in n)
 - improved backtracking, e.g., Davis--Putnam-Logemann-Loveland (DPLL)
 - heuristic search in model space (sound but incomplete)
 e.g., min-conflicts-like hill-climbing algorithms

Resolution

Conjunctive Normal Form (CNF) conjunction of disjunctions of literals

clauses E.g., (A ∨ ¬B) ∧ (B ∨ ¬C ∨ ¬D)

Resolution inference rule (for CNF):

where l_i and m_j are complementary literals. E.g., $P_{1,3} \lor P_{2,2}, \neg P_{2,2}$

 $P_{1,3}$

Resolution is sound and complete for propositional logic



Resolution

Soundness of resolution inference rule:

$$\begin{split} \neg \left(\mathit{f}_{i} \vee \ldots \vee \mathit{f}_{i-1} \vee \mathit{f}_{i+1} \vee \ldots \vee \mathit{f}_{k} \right) &\Rightarrow \mathit{f}_{i} \\ \neg \mathit{m}_{i} &\Rightarrow \left(\mathit{m}_{1} \vee \ldots \vee \mathit{m}_{i-1} \vee \mathit{m}_{i+1} \vee \ldots \vee \mathit{m}_{n} \right) \\ \neg \left(\mathit{f}_{i} \vee \ldots \vee \mathit{f}_{i-1} \vee \mathit{f}_{i+1} \vee \ldots \vee \mathit{f}_{k} \right) &\Rightarrow \left(\mathit{m}_{1} \vee \ldots \vee \mathit{m}_{i-1} \vee \mathit{m}_{i+1} \vee \ldots \vee \mathit{m}_{n} \right) \end{split}$$

Conversion to CNF

 $B_{1,1} \Leftrightarrow (P_{1,2} \vee P_{2,1})$

- 1. Eliminate \Leftrightarrow , replacing $\alpha \Leftrightarrow \beta$ with $(\alpha \Rightarrow \beta) \land (\beta \Rightarrow \alpha)$.
 - $(\mathsf{B}_{1,1} \Rightarrow (\mathsf{P}_{1,2} \vee \mathsf{P}_{2,1})) \wedge ((\mathsf{P}_{1,2} \vee \mathsf{P}_{2,1}) \Rightarrow \mathsf{B}_{1,1})$
- 2. Eliminate \Rightarrow , replacing $\alpha \Rightarrow \beta$ with $\neg \alpha \lor \beta$.
 - $(\neg \, \mathsf{B}_{1,1} \, \vee \, \mathsf{P}_{1,2} \, \vee \, \mathsf{P}_{2,1}) \, \wedge \, (\neg (\mathsf{P}_{1,2} \, \vee \, \mathsf{P}_{2,1}) \, \vee \, \mathsf{B}_{1,1})$
- 3. Move ¬ inwards using de Morgan's rules and double-negation:
- $(\neg B_{1,1} \lor P_{1,2} \lor P_{2,1}) \land ((\neg P_{1,2} \lor \neg P_{2,1}) \lor B_{1,1})$
- 4. Apply distributivity law (A over V) and flatten:
 - (¬B_{1.1} v P_{1.2} v P_{2.1}) ∧ (¬P_{1.2} v B_{1.1}) ∧ (¬P_{2.1} v B_{1.1})

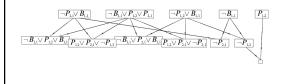
Resolution algorithm

• Proof by contradiction, i.e., show $KB \land \neg \alpha$ unsatisfiable

function PL-Resolution (KB, α) returns true or false $\mathit{clauses} \leftarrow \mathsf{the} \ \mathsf{set} \ \mathsf{of} \ \mathsf{clauses}$ in the CNF representation of $\mathit{KB} \land \neg \alpha$ $new \leftarrow \{\}$ loop do
for each C_i , C_j in clauses do resolvents \leftarrow PL-RESOLVE (C_i, C_j) if resolvents contains the empty clause then return true $new \leftarrow new \cup \ resolvents$ if $new \subseteq clauses$ then return false $clauses \leftarrow clauses \cup new$

Resolution example

• $KB = (B_{1,1} \Leftrightarrow (P_{1,2} \vee P_{2,1})) \wedge \neg B_{1,1} \alpha = \neg P_{1,2}$



Forward and backward chaining

- Horn Form (restricted) KB = conjunction of Horn clauses

 - Horn clause =
 proposition symbol; or
 (conjunction of symbols) ⇒ symbol
 E.g., C ∧ (B ⇒ A) ∧ (C ∧ D ⇒ B)
- Modus Ponens (for Horn Form): complete for Horn KBs

$$\alpha_1, \dots, \alpha_n, \qquad \alpha_1 \wedge \dots \wedge \alpha_n \Rightarrow \beta$$

- Can be used with forward chaining or backward chaining.
 These algorithms are very natural and run in linear time

Forward chaining

Idea: fire any rule whose premises are satisfied in the KB, - add its conclusion to the KB, until query is found

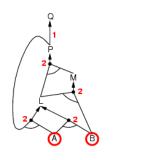
$$\begin{split} P &\Rightarrow Q \\ L \wedge M &\Rightarrow P \\ B \wedge L &\Rightarrow M \\ A \wedge P &\Rightarrow L \\ A \wedge B &\Rightarrow L \\ A \\ B \end{split}$$

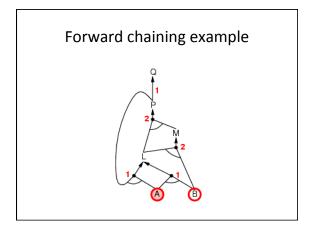


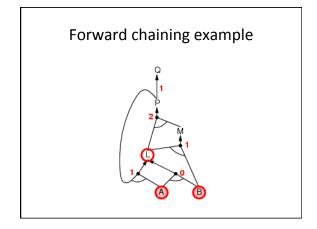
Forward chaining algorithm

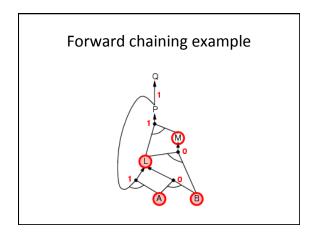
function PL-FC-ENTAILS?(KB, q) returns true or false local variables: count, a table, indexed by clause, initially the number of premises inferred, a table, indexed by symbol, each entry initially false agenda, a list of symbols, initially the symbols known to be true while agenda is not empty do $p \leftarrow Por(agenda)$ unless in/erred[p] do in/erred[p] do in/erred[p] to the for each Horn clause c in whose premise p appears do decrement count[c]
if count[c] = 0 then do
if Head[c] = q then return true
PUSH(HEAD[c], agenda)

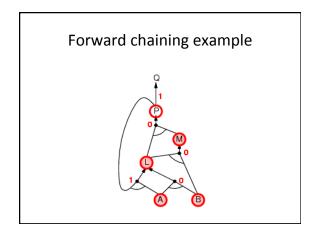
Forward chaining example

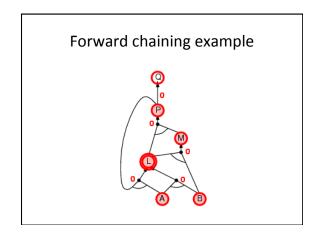


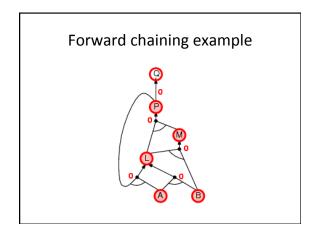












Forward chaining example

Proof of completeness

- FC derives every atomic sentence that is entailed by KB
- 1. FC reaches a fixed point where no new atomic sentences are derived
- 2. Consider the final state as a model m, assigning true/false to symbols
- 3. Every clause in the original KB is true in m

 $a_1 \wedge ... \wedge a_{k \Rightarrow} b$

- 4. Hence *m* is a model of *KB*
- 5. If $KB \models q, q$ is true in every model of KB, including m

Backward chaining

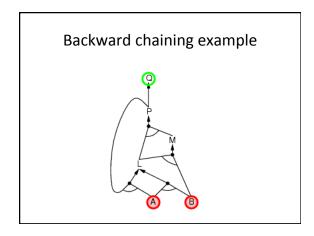
Idea: work backwards from the query q:

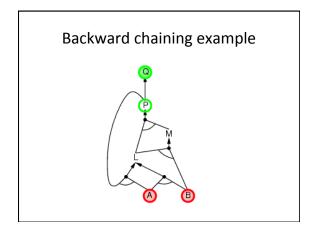
to prove q by BC, check if q is known already, or prove by BC all premises of some rule concluding q

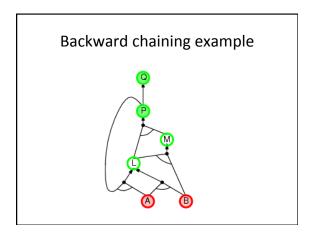
Avoid loops: check if new subgoal is already on the goal stack

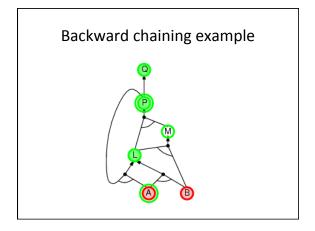
Avoid repeated work: check if new subgoal

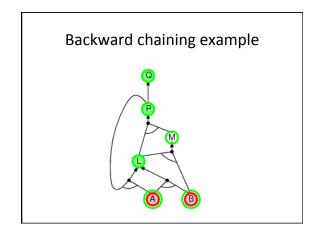
- 1. has already been proved true, or
- 2. has already failed

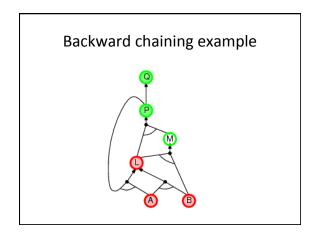


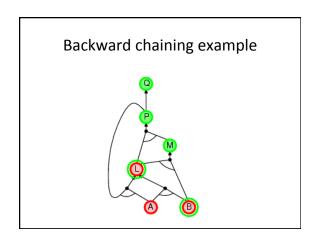


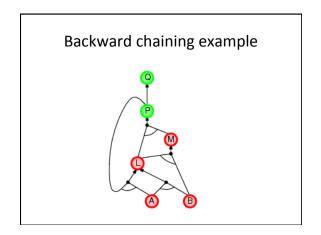


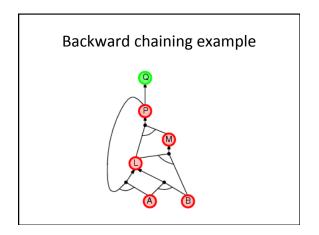




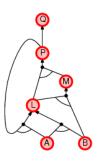








Backward chaining example



Forward vs. backward chaining

- FC is data-driven, automatic, unconscious processing, e.g., object recognition, routine decisions
- · May do lots of work that is irrelevant to the goal
- BC is goal-driven, appropriate for problem-solving, - e.g., Where are my keys? How do I get into a PhD program?
- Complexity of BC can be much less than linear in size of KB

Efficient propositional inference

Two families of efficient algorithms for propositional inference:

Complete backtracking search algorithms

- DPLL algorithm (Davis, Putnam, Logemann, Loveland)
- Incomplete local search algorithms
 - WalkSAT algorithm

The DPLL algorithm

Determine if an input propositional logic sentence (in CNF) is satisfiable

Improvements over truth table enumeration:

- Early termination
 A clause is true if any literal is true.
 A sentence is false if any clause is false.
- Pure symbol heuristic
 Pure symbol: always appears with the same "sign" in all clauses.
 e.g., In the three clauses (A v B), (–B v C), (C v A), A and B are pure, C is impure.
 Make a pure symbol literal true.
- Unit clause heuristic
 Unit clause: only one literal in the clause
 The only literal in a unit clause must be true

The DPLL algorithm

function DPLL-Satisfiable?(s) returns true or false inputs: s, a sentence in propositional logic

 $clauses \leftarrow \text{the set of clauses in the CNF representation of } s$ $symbols \leftarrow \text{a list of the proposition symbols in } s$ $\mathbf{return}\ \mathrm{DPLL}\big(\mathit{clauses}, \mathit{symbols}, []\big)$

function DPLL(clauses, symbols, model) returns true or false

if every clause in clauses is true in model then return true if every clause in clauses is true in model then return fue if some clause in clauses is false in model then return false P, value \leftarrow Find-Pure-Symbol(symbols, clauses, model) if P is non-null then return DPLL(clauses, symbols-P, |P| = value | model|) P, value \leftarrow Find-Unit-Caluses (clauses, nodel) if P is non-null then return DPLL(clauses, symbols-P, |P| = value | model|) P \leftarrow First(symbols); rest \leftarrow Rest(symbols) great \leftarrow Pirst(symbols) rest \leftarrow Pirst(symbols) great \leftarrow Pirst(symbols) great

The WalkSAT algorithm

- Incomplete, local search algorithm
- Evaluation function: The min-conflict heuristic of minimizing the number of unsatisfied clauses
- · Balance between greediness and randomness

The WalkSAT algorithm

function WALKSAT(clauses, p, max-flips) returns a satisfying model or failure inputs: clauses, a set of clauses in propositional logic p, the probability of choosing to do a "random walk" move max-flips, number of flips allowed before giving up model ← a random assignment of true/false to the symbols in clauses for i = 1 to max-flips do if model satisfies clauses then return model clause ← a randomly selected clause from clauses that is false in model with probability p flip the value in model of a randomly selected symbol from clause else flip whichever symbol in clause maximizes the number of satisfied clauses

Hard satisfiability problems

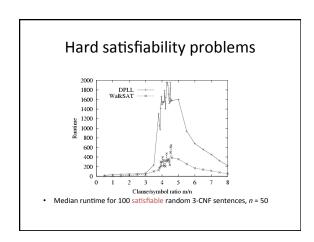
· Consider random 3-CNF sentences. e.g.,

(
$$\neg$$
 D \vee \neg B \vee C) \wedge (B \vee \neg A \vee \neg C) \wedge (\neg C \vee \neg B \vee E) \wedge (E \vee \neg D \vee B) \wedge (B \vee E \vee \neg C)

m = number of clauses n = number of symbols

- Hard problems seem to cluster near m/n = 4.3 (critical point)

Hard satisfiability problems



Inference-based agents in the wumpus world

Clause/symbol ratio m/n

A wumpus-world agent using propositional logic:

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\begin{array}{l} -P_{1,1} \\ -W_{1,1} \\ S_{x,y} \Leftrightarrow (P_{x,y+1} \vee P_{x,y+1} \vee P_{x+1,y} \vee P_{x,1,y}) \\ S_{x,y} \Leftrightarrow (W_{x,y+1} \vee W_{x,y-1} \vee W_{x+1,y} \vee W_{x+1,y}) \\ W_{1,1} \vee W_{1,2} \vee \dots \vee W_{4,4} \\ -W_{1,1} \vee -W_{1,3} \\ -W_{1,1} \vee -W_{1,3} \end{array}
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⇒ 64 distinct proposition symbols, 155 sentences

function PL-WUMPUS-AGENT (percept) returns an action inputs: percept, a list, [stench, breeze, glitter] static: KB, initially containing the "physics" of the wumpus world x, y, orientation, the agent's position (init. [1,1]) and orient. (init. right) visited, an array indicating which squares have been visited, initially false action, the agent's most recent action, initially null plan, an action sequence, initially empty update x, y, orientation, visited based on action if stench then Tell($KB, S_{x,y}$) else Tell($KB, S_{x,y}$) if prezze then Tell($KB, S_{x,y}$) else Tell($KB, S_{x,y}$) if glitter then action \leftarrow grab else if plan is nonempty then $action \leftarrow \text{POP}(plan)$ else if for some fringe square [i,j], $Ask(KB, (P_{i,j} \lor W_{i,j}))$ is true or for some fringe square [i,j], $Ask(KB, (P_{i,j} \lor W_{i,j}))$ is false then do $plan \leftarrow A^+ Graph - Search (Route-PB([x,y], orientation, [i,j], visited))$ action $\leftarrow \text{POP}(plan)$ else $action \leftarrow a$ randomly chosen move return action

Expressiveness limitation of propositional logic

- KB contains "physics" sentences for every single square
- For every time *t* and every location [*x*,*y*],
- $L_{\mathbf{x},\mathbf{y}} \wedge \mathit{FacingRight}^{\mathbf{t}} \wedge \mathit{Forward}^{\mathbf{t}} \Rightarrow L_{\mathbf{x}+1,\mathbf{y}}$
- Rapid proliferation of clauses

Summary

- Logical agents apply inference to a knowledge base to derive new information and make decisions
- Basic concepts of logic:
 - syntax: formal structure of sentences
 - semantics: truth of sentences wrt models
 - entailment: necessary truth of one sentence given another
 - inference: deriving sentences from other sentence
 - soundness: derivations produce only entailed sentences
 - completeness: derivations can produce all entailed sentences
- Wumpus world requires the ability to represent partial and negated information, reason by cases, etc.
- Resolution is complete for propositional logic Forward, backward chaining are linear-time, complete for Horn clauses
- Propositional logic lacks expressive power