

Lecture slides by Kevin Wayne
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## 1. Representative Problems

- Gale-Shapley demo


## Gale-Shapley demo

| men's preference list |  |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: |
|  | $1^{\text {st }}$ | $2^{\text {nd }}$ | $3^{\text {rd }}$ | $4^{\text {th }}$ | $5^{\text {th }}$ |
|  | Bertha | Amy | Diane | Erika | Clare |
|  | Diane | Bertha | Amy | Clare | Erika |
|  | Bertha | Erika | Clare | Diane | Amy |
|  | Amy | Diane | Clare | Bertha | Erika |
|  | Bertha | Diane | Amy | Erika | Clare |

women's preference list

|  | $1^{\text {st }}$ | 2nd | 3rd | $4^{\text {th }}$ | 5th |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Amy | Zeus | Victor | Wyatt | Yancey | Xavier |
| Bertha | Xavier | Wyatt | Yancey | Victor | Zeus |
| Clare | Wyatt | Xavier | Yancey | Zeus | Victor |
| Diane | Victor | Zeus | Yancey | Xavier | Wyatt |
| Erika | Yancey | Wyatt | Zeus | Xavier | Victor |

## Gale-Shapley demo

|  |  | men's preference list |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $1^{\text {st }}$ | 2nd $^{\text {nd }}$ | 3rd | $4^{\text {th }}$ | $5^{\text {th }}$ |  |
| Victor | Bertha | Amy | Diane | Erika | Clare |  |
| Wyatt | Diane | Bertha | Amy | Clare | Erika |  |
| Xavier | Bertha | Erika | Clare | Diane | Amy |  |
| Yancey | Amy | Diane | Clare | Bertha | Erika |  |
| Zeus | Bertha | Diane | Amy | Erika | Clare |  |

women's preference list

|  | 1 st | 2nd | 3rd | $4^{\text {th }}$ | 5th |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Amy | Zeus | Victor | Wyatt | Yancey | Xavier |
| Bertha | Xavier | Wyatt | Yancey | Victor | Zeus |
| Clare | Wyatt | Xavier | Yancey | Zeus | Victor |
| Diane | Victor | Zeus | Yancey | Xavier | Wyatt |
| Erika | Yancey | Wyatt | Zeus | Xavier | Victor |

Victor proposes to Bertha

## Gale-Shapley demo

|  | men's preference list |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: |
|  | $1^{\text {st }}$ | 2nd $^{\text {nd }}$ | 3rd | $4^{\text {th }}$ | $5^{\text {th }}$ |
| Victor | Bertha | Amy | Diane | Erika | Clare |
| Wyatt | Diane | Bertha | Amy | Clare | Erika |
| Xavier | Bertha | Erika | Clare | Diane | Amy |
| Yancey | Amy | Diane | Clare | Bertha | Erika |
| Zeus | Bertha | Diane | Amy | Erika | Clare |

women's preference list

## Gale-Shapley demo

|  |  | men's preference list |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $1^{\text {st }}$ | 2nd $^{\text {nd }}$ | 3rd | $4^{\text {th }}$ | $5^{\text {th }}$ |  |
| Victor | Bertha | Amy | Diane | Erika | Clare |  |
| Wyatt | Diane | Bertha | Amy | Clare | Erika |  |
| Xavier | Bertha | Erika | Clare | Diane | Amy |  |
| Yancey | Amy | Diane | Clare | Bertha | Erika |  |
| Zeus | Bertha | Diane | Amy | Erika | Clare |  |

women's preference list

|  | 1 st | 2nd | 3rd | 4th | 5th |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Amy | Zeus | Victor | Wyatt | Yancey | Xavier |
| Bertha | Xavier | Wyatt | Yancey | Victor | Zeus |
| Clare | Wyatt | Xavier | Yancey | Zeus | Victor |
| Diane | Victor | Zeus | Yancey | Xavier | Wyatt |
| Erika | Yancey | Wyatt | Zeus | Xavier | Victor |

Wyatt proposes to Diane

## Gale-Shapley demo

|  | men's preference list |  |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $1^{\text {st }}$ | 2nd $^{\text {nd }}$ | 3rd | $4^{\text {th }}$ | $5^{\text {th }}$ |  |
| Victor | Bertha | Amy | Diane | Erika | Clare |  |
| Wyatt | Diane | Bertha | Amy | Clare | Erika |  |
| Xavier | Bertha | Erika | Clare | Diane | Amy |  |
| Yancey | Amy | Diane | Clare | Bertha | Erika |  |
| Zeus | Bertha | Diane | Amy | Erika | Clare |  |

women's preference list
Wyatt proposes to Diane
Diane accepts
(since previously unmatched)

## Gale-Shapley demo

|  |  | men's preference list |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $1^{\text {st }}$ | 2nd $^{\text {nd }}$ | 3rd | $4^{\text {th }}$ | $5^{\text {th }}$ |  |
| Victor | Bertha | Amy | Diane | Erika | Clare |  |
| Wyatt | Diane | Bertha | Amy | Clare | Erika |  |
| Xavier | Bertha | Erika | Clare | Diane | Amy |  |
| Yancey | Amy | Diane | Clare | Bertha | Erika |  |
| Zeus | Bertha | Diane | Amy | Erika | Clare |  |

women's preference list

|  | 1 st | 2nd | 3rd | $4^{\text {th }}$ | 5th |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Amy | Zeus | Victor | Wyatt | Yancey | Xavier |
| Bertha | Xavier | Wyatt | Yancey | Victor | Zeus |
| Clare | Wyatt | Xavier | Yancey | Zeus | Victor |
| Diane | Victor | Zeus | Yancey | Xavier | Wyatt |
| Erika | Yancey | Wyatt | Zeus | Xavier | Victor |

Xavier proposes to Bertha

## Gale-Shapley demo

|  | men's preference list |  |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $1^{\text {st }}$ | 2nd $^{\text {nd }}$ | 3rd | $4^{\text {th }}$ | $5^{\text {th }}$ |  |
| Victor | Bertha | Amy | Diane | Erika | Clare |  |
| Wyatt | Diane | Bertha | Amy | Clare | Erika |  |
| Xavier | Bertha | Erika | Clare | Diane | Amy |  |
| Yancey | Amy | Diane | Clare | Bertha | Erika |  |
| Zeus | Bertha | Diane | Amy | Erika | Clare |  |


|  | women's preference list |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $1^{\text {st }}$ | 2nd | 3rd | $4^{\text {th }}$ | 5th |  |
| Amy | Zeus | Victor | Wyatt | Yancey | Xavier |  |
| Bertha | Xavier | Wyatt | Yancey | Victor | Zeus |  |
| Clare | Wyatt | Xavier | Yancey | Zeus | Victor |  |
| Diane | Victor | Zeus | Yancey | Xavier | Wyatt |  |
| Erika | Yancey | Wyatt | Zeus | Xavier | Victor |  |

## Xavier proposes to Bertha

Bertha accepts (and dumps Victor)

## Gale-Shapley demo

|  | men's preference list |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: |
|  | $1^{\text {st }}$ | 2nd $^{\text {nd }}$ | 3rd | $4^{\text {th }}$ | 5th |
| Victor | Bertha | Amy | Diane | Erika | Clare |
| Wyatt | Diane | Bertha | Amy | Clare | Erika |
| Xavier | Bertha | Erika | Clare | Diane | Amy |
| Yancey | Amy | Diane | Clare | Bertha | Erika |
| Zeus | Bertha | Diane | Amy | Erika | Clare |

women's preference list

|  | 1 st | 2nd | 3rd | 4th | 5th |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Amy | Zeus | Victor | Wyatt | Yancey | Xavier |
| Bertha | Xavier | Wyatt | Yancey | Victor | Zeus |
| Clare | Wyatt | Xavier | Yancey | Zeus | Victor |
| Diane | Victor | Zeus | Yancey | Xavier | Wyatt |
| Erika | Yancey | Wyatt | Zeus | Xavier | Victor |

## Gale-Shapley demo

| men's preference list |  |  |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $1^{\text {st }}$ | $2^{\text {nd }}$ | $3^{\text {rd }}$ | 4th $^{\text {th }}$ | 5th |  |
| Victor | Bertha | Amy | Diane | Erika | Clare |  |
| Wyatt | Diane | Bertha | Amy | Clare | Erika |  |
| Xavier | Bertha | Erika | Clare | Diane | Amy |  |
| Yancey | Amy | Diane | Clare | Bertha | Erika |  |
| Zeus | Bertha | Diane | Amy | Erika | Clare |  |

women's preference list

## Victor proposes to Amy <br> Amy accepts <br> (since previously unmatched)

## Gale-Shapley demo

| men's preference list |  |  |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $1^{\text {st }}$ | $2^{\text {nd }}$ | $3^{\text {rd }}$ | 4th $^{\text {th }}$ | 5th |  |
| Victor | Bertha | Amy | Diane | Erika | Clare |  |
| Wyatt | Diane | Bertha | Amy | Clare | Erika |  |
| Xavier | Bertha | Erika | Clare | Diane | Amy |  |
| Yancey | Amy | Diane | Clare | Bertha | Erika |  |
| Zeus | Bertha | Diane | Amy | Erika | Clare |  |

women's preference list

|  | 1 st | 2nd | 3rd | $4^{\text {th }}$ | 5th |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Amy | Zeus | Victor | Wyatt | Yancey | Xavier |
| Bertha | Xavier | Wyatt | Yancey | Victor | Zeus |
| Clare | Wyatt | Xavier | Yancey | Zeus | Victor |
| Diane | Victor | Zeus | Yancey | Xavier | Wyatt |
| Erika | Yancey | Wyatt | Zeus | Xavier | Victor |

## Gale-Shapley demo

| men's preference list |  |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: |
|  | $1^{\text {st }}$ | 2nd $^{\text {nd }}$ | 3rd | $4^{\text {th }}$ | $5^{\text {th }}$ |
|  | Bertha | Amy | Diane | Erika | Clare |
|  | Diane | Bertha | Amy | Clare | Erika |
|  | Bertha | Erika | Clare | Diane | Amy |
|  | Amy | Diane | Clare | Bertha | Erika |
|  | Bertha | Diane | Amy | Erika | Clare |

women's preference list

|  | 1 st | 2nd | 3rd | 4th | 5th |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Amy | Zeus | Victor | Wyatt | Yancey | Xavier |
| Bertha | Xavier | Wyatt | Yancey | Victor | Zeus |
| Clare | Wyatt | Xavier | Yancey | Zeus | Victor |
| Diane | Victor | Zeus | Yancey | Xavier | Wyatt |
| Erika | Yancey | Wyatt | Zeus | Xavier | Victor |

Yancey proposes to Amy
Amy rejects (since she prefers Victor)

## Gale-Shapley demo

|  | men's preference list |  |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $1^{\text {st }}$ | 2nd $^{\text {nd }}$ | 3rd | $4^{\text {th }}$ | 5th |  |
| Victor | Bertha | Amy | Diane | Erika | Clare |  |
| Wyatt | Diane | Bertha | Amy | Clare | Erika |  |
| Xavier | Bertha | Erika | Clare | Diane | Amy |  |
| Yancey | Amy | Diane | Clare | Bertha | Erika |  |
| Zeus | Bertha | Diane | Amy | Erika | Clare |  |

women's preference list

|  | 1 st | 2nd | 3rd | 4th | 5th |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Amy | Zeus | Victor | Wyatt | Yancey | Xavier |
| Bertha | Xavier | Wyatt | Yancey | Victor | Zeus |
| Clare | Wyatt | Xavier | Yancey | Zeus | Victor |
| Diane | Victor | Zeus | Yancey | Xavier | Wyatt |
| Erika | Yancey | Wyatt | Zeus | Xavier | Victor |

# Yancey proposes to Diane 

## Gale-Shapley demo

|  | men's preference list |  |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $1^{\text {st }}$ | 2nd $^{\text {nd }}$ | 3rd | $4^{\text {th }}$ | $5^{\text {th }}$ |  |
| Victor | Bertha | Amy | Diane | Erika | Clare |  |
| Wyatt | Diane | Bertha | Amy | Clare | Erika |  |
| Xavier | Bertha | Erika | Clare | Diane | Amy |  |
| Yancey | Amy | Diane | Clare | Bertha | Erika |  |
| Zeus | Bertha | Diane | Amy | Erika | Clare |  |


|  | women's preference list |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1 st | 2nd | 3rd | 4th | 5th |
| Amy | Zeus | Victor | Wyatt | Yancey | Xavier |
| Bertha | Xavier | Wyatt | Yancey | Victor | Zeus |
| Clare | Wyatt | Xavier | Yancey | Zeus | Victor |
| Diane | Victor | Zeus | Yancey | Xavier | Wyatt |
| Erika | Yancey | Wyatt | Zeus | Xavier | Victor |

## Yancey proposes to Diane <br> Dianne accepts (and dumps Wyatt)

## Gale-Shapley demo

|  | men's preference list |  |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $1^{\text {st }}$ | 2nd $^{\text {nd }}$ | 3rd | $4^{\text {th }}$ | 5th |  |
| Victor | Bertha | Amy | Diane | Erika | Clare |  |
| Wyatt | Diane | Bertha | Amy | Clare | Erika |  |
| Xavier | Bertha | Erika | Clare | Diane | Amy |  |
| Yancey | Amy | Diane | Clare | Bertha | Erika |  |
| Zeus | Bertha | Diane | Amy | Erika | Clare |  |

women's preference list

|  | 1 st | 2nd | 3rd | 4th | 5th |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Amy | Zeus | Victor | Wyatt | Yancey | Xavier |
| Bertha | Xavier | Wyatt | Yancey | Victor | Zeus |
| Clare | Wyatt | Xavier | Yancey | Zeus | Victor |
| Diane | Victor | Zeus | Yancey | Xavier | Wyatt |
| Erika | Yancey | Wyatt | Zeus | Xavier | Victor |

## Gale-Shapley demo

|  | men's preference list |  |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $1^{\text {st }}$ | 2nd $^{\text {nd }}$ | 3rd | $4^{\text {th }}$ | $5^{\text {th }}$ |  |
| Victor | Bertha | Amy | Diane | Erika | Clare |  |
| Wyatt | Diane | Bertha | Amy | Clare | Erika |  |
| Xavier | Bertha | Erika | Clare | Diane | Amy |  |
| Yancey | Amy | Diane | Clare | Bertha | Erika |  |
| Zeus | Bertha | Diane | Amy | Erika | Clare |  |


|  | women's preference list |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1 st | 2nd | 3rd | 4th | 5th |
| Amy | Zeus | Victor | Wyatt | Yancey | Xavier |
| Bertha | Xavier | Wyatt | Yancey | Victor | Zeus |
| Clare | Wyatt | Xavier | Yancey | Zeus | Victor |
| Diane | Victor | Zeus | Yancey | Xavier | Wyatt |
| Erika | Yancey | Wyatt | Zeus | Xavier | Victor |

# Wyatt proposes to Bertha <br> Bertha rejects (since she prefers Xavier) 

## Gale-Shapley demo

|  | men's preference list |  |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $1^{\text {st }}$ | 2nd $^{\text {nd }}$ | 3rd | $4^{\text {th }}$ | 5th |  |
| Victor | Bertha | Amy | Diane | Erika | Clare |  |
| Wyatt | Diane | Bertha | Amy | Clare | Erika |  |
| Xavier | Bertha | Erika | Clare | Diane | Amy |  |
| Yancey | Amy | Diane | Clare | Bertha | Erika |  |
| Zeus | Bertha | Diane | Amy | Erika | Clare |  |

women's preference list

|  | 1 1st | 2nd | 3rd | 4th | 5th |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Amy | Zeus | Victor | Wyatt | Yancey | Xavier |
| Bertha | Xavier | Wyatt | Yancey | Victor | Zeus |
| Clare | Wyatt | Xavier | Yancey | Zeus | Victor |
| Diane | Victor | Zeus | Yancey | Xavier | Wyatt |
| Erika | Yancey | Wyatt | Zeus | Xavier | Victor |

## Gale-Shapley demo

|  | men's preference list |  |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $1^{\text {st }}$ | 2nd $^{\text {nd }}$ | 3rd | $4^{\text {th }}$ | $5^{\text {th }}$ |  |
| Victor | Bertha | Amy | Diane | Erika | Clare |  |
| Wyatt | Diane | Bertha | Amy | Clare | Erika |  |
| Xavier | Bertha | Erika | Clare | Diane | Amy |  |
| Yancey | Amy | Diane | Clare | Bertha | Erika |  |
| Zeus | Bertha | Diane | Amy | Erika | Clare |  |

women's preference list

|  | 1 st | 2nd | 3rd | 4th | 5th |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Amy | Zeus | Victor | Wyatt | Yancey | Xavier |
| Bertha | Xavier | Wyatt | Yancey | Victor | Zeus |
| Clare | Wyatt | Xavier | Yancey | Zeus | Victor |
| Diane | Victor | Zeus | Yancey | Xavier | Wyatt |
| Erika | Yancey | Wyatt | Zeus | Xavier | Victor |

## Gale-Shapley demo

|  | men's preference list |  |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $1^{\text {st }}$ | 2nd $^{\text {nd }}$ | 3rd | $4^{\text {th }}$ | $5^{\text {th }}$ |  |
| Victor | Bertha | Amy | Diane | Erika | Clare |  |
| Wyatt | Diane | Bertha | Amy | Clare | Erika |  |
| Xavier | Bertha | Erika | Clare | Diane | Amy |  |
| Yancey | Amy | Diane | Clare | Bertha | Erika |  |
| Zeus | Bertha | Diane | Amy | Erika | Clare |  |

women's preference list

|  | 1 st | 2nd | 3rd | 4th | 5th |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Amy | Zeus | Victor | Wyatt | Yancey | Xavier |
| Bertha | Xavier | Wyatt | Yancey | Victor | Zeus |
| Clare | Wyatt | Xavier | Yancey | Zeus | Victor |
| Diane | Victor | Zeus | Yancey | Xavier | Wyatt |
| Erika | Yancey | Wyatt | Zeus | Xavier | Victor |

## Gale-Shapley demo

|  | men's preference list |  |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $1^{\text {st }}$ | 2nd $^{\text {nd }}$ | 3rd | $4^{\text {th }}$ | $5^{\text {th }}$ |  |
| Victor | Bertha | Amy | Diane | Erika | Clare |  |
| Wyatt | Diane | Bertha | Amy | Clare | Erika |  |
| Xavier | Bertha | Erika | Clare | Diane | Amy |  |
| Yancey | Amy | Diane | Clare | Bertha | Erika |  |
| Zeus | Bertha | Diane | Amy | Erika | Clare |  |


|  | women's preference list |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1 st | 2nd | 3rd | 4th | 5th |
| Amy | Zeus | Victor | Wyatt | Yancey | Xavier |
| Bertha | Xavier | Wyatt | Yancey | Victor | Zeus |
| Clare | Wyatt | Xavier | Yancey | Zeus | Victor |
| Diane | Victor | Zeus | Yancey | Xavier | Wyatt |
| Erika | Yancey | Wyatt | Zeus | Xavier | Victor |

Wyatt proposes to Clare
Clare accepts
(since previously unmatched)

## Gale-Shapley demo

| men's preference list |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1 st | 2nd | 3rd | 4th | 5th |  |
| Victor | Bertha | Amy | Diane | Erika | Clare |  |
| Wyatt | Diane | Bertha | Amy | Clare | Erika |  |
| Xavier | Bertha | Erika | Clare | Diane | Amy |  |
| Yancey | Amy | Diane | Clare | Bertha | Erika |  |
| Zeus | Bertha | Diane | Amy | Erika | Clare |  |


|  | women's preference list |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1 st | 2nd | 3rd | 4th | 5th |
| Amy | Zeus | Victor | Wyatt | Yancey | Xavier |
| Bertha | Xavier | Wyatt | Yancey | Victor | Zeus |
| Clare | Wyatt | Xavier | Yancey | Zeus | Victor |
| Diane | Victor | Zeus | Yancey | Xavier | Wyatt |
| Erika | Yancey | Wyatt | Zeus | Xavier | Victor |

## Zeus proposes to Bertha

## Gale-Shapley demo

|  | men's preference list |  |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $1^{\text {st }}$ | 2nd $^{\text {nd }}$ | 3rd | $4^{\text {th }}$ | $5^{\text {th }}$ |  |
| Victor | Bertha | Amy | Diane | Erika | Clare |  |
| Wyatt | Diane | Bertha | Amy | Clare | Erika |  |
| Xavier | Bertha | Erika | Clare | Diane | Amy |  |
| Yancey | Amy | Diane | Clare | Bertha | Erika |  |
| Zeus | Bertha | Diane | Amy | Erika | Clare |  |


|  | women's preference list |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1 st | 2nd | 3rd | 4th | 5th |
| Amy | Zeus | Victor | Wyatt | Yancey | Xavier |
| Bertha | Xavier | Wyatt | Yancey | Victor | Zeus |
| Clare | Wyatt | Xavier | Yancey | Zeus | Victor |
| Diane | Victor | Zeus | Yancey | Xavier | Wyatt |
| Erika | Yancey | Wyatt | Zeus | Xavier | Victor |

## Gale-Shapley demo

|  | men's preference list |  |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $1^{\text {st }}$ | 2nd $^{\text {nd }}$ | 3rd | $4^{\text {th }}$ | 5th |  |
| Victor | Bertha | Amy | Diane | Erika | Clare |  |
| Wyatt | Diane | Bertha | Amy | Clare | Erika |  |
| Xavier | Bertha | Erika | Clare | Diane | Amy |  |
| Yancey | Amy | Diane | Clare | Bertha | Erika |  |
| Zeus | Bertha | Diane | Amy | Erika | Clare |  |

women's preference list

|  | 1 st | 2nd | 3rd | 4th | 5th |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Amy | Zeus | Victor | Wyatt | Yancey | Xavier |
| Bertha | Xavier | Wyatt | Yancey | Victor | Zeus |
| Clare | Wyatt | Xavier | Yancey | Zeus | Victor |
| Diane | Victor | Zeus | Yancey | Xavier | Wyatt |
| Erika | Yancey | Wyatt | Zeus | Xavier | Victor |

# Zeus proposes to Diane 

## Gale-Shapley demo

|  | men's preference list |  |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $1^{\text {st }}$ | 2nd $^{\text {nd }}$ | 3rd | $4^{\text {th }}$ | $5^{\text {th }}$ |  |
| Victor | Bertha | Amy | Diane | Erika | Clare |  |
| Wyatt | Diane | Bertha | Amy | Clare | Erika |  |
| Xavier | Bertha | Erika | Clare | Diane | Amy |  |
| Yancey | Amy | Diane | Clare | Bertha | Erika |  |
| Zeus | Bertha | Diane | Amy | Erika | Clare |  |

women's preference list

|  | 1 st | 2nd | 3rd | 4th | 5th |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Amy | Zeus | Victor | Wyatt | Yancey | Xavier |
| Bertha | Xavier | Wyatt | Yancey | Victor | Zeus |
| Clare | Wyatt | Xavier | Yancey | Zeus | Victor |
| Diane | Victor | Zeus | Yancey | Xavier | Wyatt |
| Erika | Yancey | Wyatt | Zeus | Xavier | Victor |

# Zeus proposes to Diane <br> Diane accepts (and dumps Yancey) 

## Gale-Shapley demo

|  | men's preference list |  |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $1^{\text {st }}$ | 2nd $^{\text {nd }}$ | 3rd | $4^{\text {th }}$ | 5th |  |
| Victor | Bertha | Amy | Diane | Erika | Clare |  |
| Wyatt | Diane | Bertha | Amy | Clare | Erika |  |
| Xavier | Bertha | Erika | Clare | Diane | Amy |  |
| Yancey | Amy | Diane | Clare | Bertha | Erika |  |
| Zeus | Bertha | Diane | Amy | Erika | Clare |  |

women's preference list

|  | 1 st | 2nd | 3rd | $4^{\text {th }}$ | 5th |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Amy | Zeus | Victor | Wyatt | Yancey | Xavier |
| Bertha | Xavier | Wyatt | Yancey | Victor | Zeus |
| Clare | Wyatt | Xavier | Yancey | Zeus | Victor |
| Diane | Victor | Zeus | Yancey | Xavier | Wyatt |
| Erika | Yancey | Wyatt | Zeus | Xavier | Victor |

Yancey proposes to Clare

## Gale-Shapley demo

| men's preference list |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $1^{\text {st }}$ | 2nd | 3rd | 4th | 5th |  |
| Victor | Bertha | Amy | Diane | Erika | Clare |  |
| Wyatt | Diane | Bertha | Amy | Clare | Erika |  |
| Xavier | Bertha | Erika | Clare | Diane | Amy |  |
| Yancey | Amy | Diane | Clare | Bertha | Erika |  |
| Zeus | Bertha | Diane | Amy | Erika | Clare |  |

women's preference list

|  | 1 st | 2nd | 3rd | $4^{\text {th }}$ | 5th |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Amy | Zeus | Victor | Wyatt | Yancey | Xavier |
| Bertha | Xavier | Wyatt | Yancey | Victor | Zeus |
| Clare | Wyatt | Xavier | Yancey | Zeus | Victor |
| Diane | Victor | Zeus | Yancey | Xavier | Wyatt |
| Erika | Yancey | Wyatt | Zeus | Xavier | Victor |

# Yancey proposes to Clare <br> Clare rejects (since she prefers Wyatt) 

## Gale-Shapley demo

|  | men's preference list |  |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $1^{\text {st }}$ | 2nd $^{\text {nd }}$ | 3rd | $4^{\text {th }}$ | 5th |  |
| Victor | Bertha | Amy | Diane | Erika | Clare |  |
| Wyatt | Diane | Bertha | Amy | Clare | Erika |  |
| Xavier | Bertha | Erika | Clare | Diane | Amy |  |
| Yancey | Amy | Diane | Clare | Bertha | Erika |  |
| Zeus | Bertha | Diane | Amy | Erika | Clare |  |

women's preference list

|  | 1 st | 2nd | 3rd | 4th | 5th |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Amy | Zeus | Victor | Wyatt | Yancey | Xavier |
| Bertha | Xavier | Wyatt | Yancey | Victor | Zeus |
| Clare | Wyatt | Xavier | Yancey | Zeus | Victor |
| Diane | Victor | Zeus | Yancey | Xavier | Wyatt |
| Erika | Yancey | Wyatt | Zeus | Xavier | Victor |

Yancey proposes to Bertha

## Gale-Shapley demo

|  | men's preference list |  |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $1^{\text {st }}$ | 2nd $^{\text {nd }}$ | 3rd | $4^{\text {th }}$ | 5th |  |
| Victor | Bertha | Amy | Diane | Erika | Clare |  |
| Wyatt | Diane | Bertha | Amy | Clare | Erika |  |
| Xavier | Bertha | Erika | Clare | Diane | Amy |  |
| Yancey | Amy | Diane | Clare | Bertha | Erika |  |
| Zeus | Bertha | Diane | Amy | Erika | Clare |  |

women's preference list

|  | 1 st | 2nd | 3rd | $4^{\text {th }}$ | 5th |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Amy | Zeus | Victor | Wyatt | Yancey | Xavier |
| Bertha | Xavier | Wyatt | Yancey | Victor | Zeus |
| Clare | Wyatt | Xavier | Yancey | Zeus | Victor |
| Diane | Victor | Zeus | Yancey | Xavier | Wyatt |
| Erika | Yancey | Wyatt | Zeus | Xavier | Victor |

> Yancey proposes to Bertha
> Bertha rejects (since she prefers Xavier)

## Gale-Shapley demo

|  | men's preference list |  |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $1^{\text {st }}$ | $2^{\text {nd }}$ | 3rd $^{\text {rd }}$ | 4th | 5th |  |
| Victor | Bertha | Amy | Diane | Erika | Clare |  |
| Wyatt | Diane | Bertha | Amy | Clare | Erika |  |
| Xavier | Bertha | Erika | Clare | Diane | Amy |  |
| Yancey | Amy | Diane | Clare | Bertha | Erika |  |
| Zeus | Bertha | Diane | Amy | Erika | Clare |  |


|  | women's preference list |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1 st | $2^{\text {nd }}$ | 3rd | $4^{\text {th }}$ | 5th |
| Amy | Zeus | Victor | Wyatt | Yancey | Xavier |
| Bertha | Xavier | Wyatt | Yancey | Victor | Zeus |
| Clare | Wyatt | Xavier | Yancey | Zeus | Victor |
| Diane | Victor | Zeus | Yancey | Xavier | Wyatt |
| Erika | Yancey | Wyatt | Zeus | Xavier | Victor |

## Gale-Shapley demo

|  | men's preference list |  |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1 st | 2nd | 3rd | 4th | 5th |  |
| Victor | Bertha | Amy | Diane | Erika | Clare |  |
| Wyatt | Diane | Bertha | Amy | Clare | Erika |  |
| Xavier | Bertha | Erika | Clare | Diane | Amy |  |
| Yancey | Amy | Diane | Clare | Bertha | Erika |  |
| Zeus | Bertha | Diane | Amy | Erika | Clare |  |

women's preference list

|  | $1^{\text {st }}$ | $2^{\text {nd }}$ | 3rd | $4^{\text {th }}$ | 5th |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Amy | Zeus | Victor | Wyatt | Yancey | Xavier |
| Bertha | Xavier | Wyatt | Yancey | Victor | Zeus |
| Clare | Wyatt | Xavier | Yancey | Zeus | Victor |
| Diane | Victor | Zeus | Yancey | Xavier | Wyatt |
| Erika | Yancey | Wyatt | Zeus | Xavier | Victor |

## Gale-Shapley demo

| men's preference list |  |  |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $1^{\text {st }}$ | $2^{\text {nd }}$ | 3rd | 4th | 5th |  |
| Victor | Bertha | Amy | Diane | Erika | Clare |  |
| Wyatt | Diane | Bertha | Amy | Clare | Erika |  |
| Xavier | Bertha | Erika | Clare | Diane | Amy |  |
| Yancey | Amy | Diane | Clare | Bertha | Erika |  |
| Zeus | Bertha | Diane | Amy | Erika | Clare |  |

women's preference list

|  | $1^{\text {st }}$ | $2^{\text {nd }}$ | 3rd | $4^{\text {th }}$ | 5th |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Amy | Zeus | Victor | Wyatt | Yancey | Xavier |
| Bertha | Xavier | Wyatt | Yancey | Victor | Zeus |
| Clare | Wyatt | Xavier | Yancey | Zeus | Victor |
| Diane | Victor | Zeus | Yancey | Xavier | Wyatt |
| Erika | Yancey | Wyatt | Zeus | Xavier | Victor |

