

## Math 2300

### Selected Definitions from Section 2.1:

p.38

A **statement** (or **proposition**) is a sentence that is true or false but not both.

p.42

A **statement form** (or **propositional form**) is an expression made up of statement variables (such as  $p$ ,  $q$ , and  $r$ ) and logical connectives (such as  $\sim$ ,  $\wedge$ , and  $\vee$ ) that becomes a statement when actual statements are substituted for the component statement variables.

The **truth table** for a given *statement form* displays the truth values that correspond to all possible combinations of truth values for its component statement variables.

p.44

Two *statement forms* are called **logically equivalent** if, and only if, they have identical truth values for each possible substitution of statements for their statement variables. The logical equivalence of statement forms  $P$  and  $Q$  is denoted by writing  $P \equiv Q$ .

Two *statements* are called logically equivalent if, and only if, they have logically equivalent forms when identical component statement variables are used to replace identical component statements.

p.48

A **tautology** is a *statement form* that is always true regardless of the truth values of the individual statements substituted for its statement variables. A statement whose form is a tautology is a **tautological statement**.

A **contradiction** is a *statement form* that is always false regardless of the truth values of the individual statements substituted for its statement variables. A statement whose form is a contradiction is a **contradictory statement**.